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New quaternary amorphous materials
Si-B-C-N: reactive magnetron sputtering and
an ab-initio study

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I submit for examining and defending a thesis written at the Faculty of Applied Sciences, University of West Bohemia (Czech Republic) and at The School of Physics, Faculty of Science, University of Sydney (Australia).

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To the best of my knowledge, this thesis contains no copy or paraphrase of work published by any other person, except where duly acknowledged in the text.

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Chapter 1 - Introduction

1 Introduction

Si-B-C-N materials are currently attracting a great deal of international interest due to their high hardness and exceptional thermal stability. This combination of properties indicates that these materials may have great potential in applications such as coatings technologies, microelectronics or production of thermally stable fibres for composites. This thesis describes experimental preparation of new hard and highly thermally stable amorphous Si-B-C-N materials, and computer simulations of their structures to aid in the understanding of physical mechanisms governing their synthesis and properties. This chapter includes motivation of the research (description of predecessors of these materials), status of knowledge concerning both experimental preparation of Si-B-C-N materials and the computer simulations, and list of particular aims of the thesis.

1.1 Hard amorphous materials

In 1980's started a boom concerning high-performance advanced ceramics and their mechanical, thermal and electrical applications. Various properties of these new hard materials have been studied by both experimental and theoretical methods. In bulk form they can for example potentially serve as structural parts of automotive engines or turbines up to very high temperatures. In the form of thin films they can for example maximize hardness of the surface or optimize its wear resistance without sacrificing properties (such as toughness) of the bulk material.

The $\beta$-C$_3$N$_4$ material (with structure derived from $\beta$-Si$_3$N$_4$) was predicted to have hardness comparable or even higher than diamond. Although all attempts to synthesize the superhard crystalline $\beta$-C$_3$N$_4$ phase have thus far been unsuccessful, but have resulted in several different kinds of carbon nitride (CN$_x$) compounds. In spite of the fact that most of the CN$_x$ films prepared by various techniques are amorphous and substoichiometric in nitrogen, these layers can possess interesting and potentially very useful mechanical properties, such as high hardness, very large elastic recovery, good adhesion to substrates and low friction coefficient and wear.

Later, the ternary Si-C-N materials attracted great interest due to their new features compared to those of crystalline Si$_3$N$_4$ and SiC mixtures and their potential applications in microelectronics and coating technologies. Various deposition techniques were used to prepare crystalline, amorphous or nanostructured Si-C-N compounds. These materials can possess a useful combination of properties, such as high hardness, wide band gap characteristics, a wide optical transparency window, promising field emission characteristics, high-temperature oxidation resistance, chemical inertness and promising wetting behavior.

Recently, it has been reported that addition of proper amount of boron into Si-C-N system leads to a new unique class of Si-B-C-N ceramics, combining an exceptional high-temperature behaviour (oxidation resistance, creep resistance, stability of mechanical properties, etc.) with same or even better other material characteristics than possess binary and ternary materials from the respective subsystems. List of all achievements in this field, together with all references available, is provided in the following separate section 1.2.1.
1.2 Status of knowledge

1.2.1 Experimental preparation of Si-B-C-N materials

Si-B-C-N materials can possess very high hardness due to the formation of a high volume density of short covalent bonds. Moreover, proper amount of boron decreases activity of carbon integrated in B-C-N zones in comparison with "free carbon" and thus dramatically increases their thermal stability in comparison with the Si-C-N materials\textsuperscript{11,12}. This is due to the increase of temperatures when start the decomposition reactions $\text{Si}_3\text{N}_4 + 3\text{C} \rightarrow 3\text{SiC} + 2\text{N}_2$ and $\text{Si}_3\text{N}_4 \rightarrow 3\text{Si} + 2\text{N}_2$ (under 1 atmosphere of $\text{N}_2$: 1481 and 1840 °C, respectively) to higher values. Unique combination of these features with the other properties reported previously for binary and ternary materials from this system lead to many potential applications in areas such as:

- coating technologies\textsuperscript{13,14}.
- microelectronics\textsuperscript{14,15}.
- production of thermally stable fibres for composites\textsuperscript{16}.

In recent years, materials have been already reported that feature at various elemental compositions one or more of:

- very high thermal stability and oxidation resistance\textsuperscript{11-13,16-26}.
- creep resistance at elevated temperatures\textsuperscript{22,27,28}.
- low stress\textsuperscript{29}.
- low thermal expansion coefficient\textsuperscript{19,23}.
- low thermal conductivity\textsuperscript{23}.
- homogeneity leading to a smooth surface\textsuperscript{14,16,18,22}.
- promising electrical properties (significantly lower resistivity than the Si-C-N ceramics)\textsuperscript{15}.
- transparency and good adherence to substrates.

Most of recently published works on Si-B-C-N materials deal with preparation of Si-B-C-N ceramics by precursor pyrolysis\textsuperscript{11,12,15-21,23-28,30-38}. Despite the number of valuable results obtained, this method has disadvantages including degradation of properties due to the large content of hydrogen from the precursors in materials and high process temperatures, let alone industrial applications of materials produced in the form of small porous grains\textsuperscript{21}. Fewer works deal with preparation of Si-B-C-N materials in the form of thin films by CVD\textsuperscript{13,14,29}. Also this method uses the hydrogen-containing precursors.

To our knowledge, up to now, no effort has been made to form Si–B–C–N films using magnetron sputtering (or any other PVD method), which allows film generation at noticeably reduced substrate temperatures and without hydrogen-containing precursors resulting in an enlarged residual content of hydrogen in films. The only exceptions are our recent papers\textsuperscript{39-41}. Some of these results (including results on thermal stability and oxidation resistance) were also included in recent PhD theses – Refs. 42 and 43. Other part of results published in these papers form basis of chapters 3 and 4 of this thesis. In the following list are included all characteristics of our Si-B-C-N materials prepared by reactive magnetron sputtering in the form of thin films. The films were found to have the following main characteristics:
• density around 2.4 g/cm$^3$.
• amorphicity (HRTEM, SAED).
• optical transparency for some compositions (ellipsometry).
• exclusive bonding of B and preferable bonding of Si and C to N (XPS, IR VASE).
• extremely high oxidation resistance in air, for some compositions up to a 1350 °C substrate limit (TGA).
• hardness up to 47 GPa, modified Young modulus between 170 and 270 GPa and elastic recovery around 75 % (nanoindentation).
• good adhesion to substrates at compressive stress lower than 1.8 GPa (profilometry).
• friction coefficients around 0.4 (tribometry).
• electrical conductivity for some compositions comparable with semiconductors (four points method).

1.2.2 *Ab-initio simulations of amorphous materials*

In connection with increased computing possibilities in last years, the molecular-dynamics (MD) simulations became a well established tool, which can support an experiment by providing information not accessible experimentally. Many different levels of theory can be used to describe the interatomic interactions, ranging from density-functional theory (DFT), through the tight-binding approaches, to empirical potential methods. An overview of them together with comparison of their results with experiment can be found in Ref. 44.

Because internal network structure and material properties of amorphous solids are intensively dependent on the formation conditions (the cooling rate of the liquid quench and the ordering processes that occur while the material solidifies from the melt), meaningful computer simulations of this type of material must focus on the formation process. In our simulation work, we try to capture this formation process using a *liquid quench* algorithm. This technique attempts to capture the formation conditions of the real materials, which arise from rapid cooling of the localized melt (*thermal spike*) created around sites of energetic ion impact. This method has been successfully applied to various amorphous materials including carbon$^{45-47}$, H:C$^{48}$, C doped by N$^{49}$, (B)(Al)N$^{50}$ or H:SiC$^{51}$.

Informations accessible in principle using the ab-initio methods (particularly the Car-Parrinello implementation of density functional theory) include:

- structural data such as bond statistics, bond lengths, bond orders, atomic coordinations, roles of various types of atoms or segregation in materials.
- calculations of various temperature-dependent characteristics. The ability to "see" the atomic motion can contribute greatly to the understanding of the mechanisms of many dynamical phenomena.
- values of various physical (and chemical) properties. Because it is only the adiabatic motion of the ground state that is calculated directly, information on electronically excited states (and hence on properties such as the conductivity) can only be obtained after further calculations. The ground-state electron density resulting from DFT MD calculations may be an useful input for them$^{52}$. The calculable properties include
  - density of states, band structure and charge densities,
  - elastic constants and ideal strength,
  - optical conductivity,
  - magnetic properties,
  - vibrational (infrared) frequencies,
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- or neutron-diffraction data.

1.3 Aims of the thesis

Our research was originally started as a purely experimental work in the field of preparation and characterization of materials from the Si-B-C-N system by magnetron sputtering (see the aims in the following section 1.3.1). Due to a number of complex relations between experimental conditions, elemental composition and structure and properties of these quaternary materials, a combined approach of experiment and computer simulations has been later used to find and explain them. This necessarily led to further aims listed in the section 1.3.2.

1.3.1 Aims of the experimental part

First part of the thesis is focused on experimental preparation of new hard quaternary amorphous materials Si-B-C-N in the form of thin films. To our knowledge, up to now, no effort has been made to form Si–B–C–N films using magnetron sputtering except our recent papers39-41. This technique allows film generation at noticeably reduced substrate temperatures and without hydrogen-containing precursors resulting in an enlarged residual content of hydrogen in films. Let us recall that the magnetron sputtering is one of the most versatile techniques compatible with semiconductor technologies and that its further important advantage is an easy up-scaling. Specific aims of this part of the thesis were to:

(1) master preparation of Si-B-C-N thin films using magnetron sputtering of composite C-Si-B and B₄C-Si targets in N₂ + Ar gas mixtures on rf-biased substrates at low substrate temperatures, and measurements of their mechanical properties (hardness, compressive stress, effective Young's modulus, elastic recovery) and electrical conductivity.

(2) deposit a series of samples by changing sputtered target composition and gas mixture composition, and to show and explain relationships of process parameters, elemental composition, bonding structure and properties of deposited Si-B-C-N films.

(3) show and explain the effect of rf-induced negative substrate bias voltage on the film characteristics (elemental composition, bonding structure, mechanical and electrical properties) for several most promising sputtered target compositions and gas mixture compositions identified.

(4) calculate deposition characteristics (such as a ratio of fluxes of ions and film-forming particles bombarding the growing films, and an energy delivered into deposited films per one film atom), and to use them for explaining the effect of substrate bias voltage.

1.3.2 Aims of the theoretical part

Second part of the thesis is focused on ab-initio simulations of structures of experimentally prepared Si-B-C-N materials (with small content of implanted Ar). In the performed liquid-quench simulations, the Kohn-Sham equations for the valence electrons are expanded in a basis of plane wave functions, while core electrons were represented using Goedecker-type pseudopotentials. We simplified the ion bombardment process by assuming that the primary impact creates a localized region of high temperature, commonly referred to as a thermal spike. Thermal spikes have a cooling time sufficiently short to be simulated using ab initio molecular dynamics (MD) methods. Specific aims of this part of the thesis were to:
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(1) master running of MD simulations using the Car-Parrinello Molecular Dynamics (CPMD) code, and the liquid-quench algorithm which attempts to capture the formation conditions of the real materials arising from rapid cooling of the localized melt (thermal spike) created around sites of energetic ion impact.

(2) perform series of liquid-quench simulations of nitrogen-containing amorphous (Si)-(B)-C-N materials in order to examine formation of N₂ molecules during these simulations, in order to show dependence of this effect on temperature, material density and cooling time of the thermal spike, and to propose an simulation algorithm which accounts for N₂ formation and diffusion out of the structure and still yields a material of desired N-content.

(3) investigate how the presence of Ar atoms in the sample affects the liquid quench and the final structure of the Si-B-C-N materials, and to use the simulation results for explaining related experimental results on deposited samples containing implanted Ar atoms.

(4) calculate various data affecting material properties (such as bonding statistics or electronic structure), to compare them for previously deposited materials of different Si-B-C-N compositions in order to show resources and limits of the simulation method used, and to use the simulation results for explaining related experimental results on deposited samples.

1.4 References

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41 J. Čížek, J. Vlček, L. Martinů, A. Amassian, Š. Potocký, J. Houška and Z. Soukup, prepared for publication in Thin Solid Films
44 N. Cooper, Molecular Dynamics Simulations of Amorphous Silicon Carbon Alloys, Ph.D. thesis (The University of Sydney, 2004).

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2 Methodology

First part of this chapter describes in detail reactive magnetron sputtering of Si-B-C-N materials, evaluating of process characteristics and measurements of properties of Si-B-C-N materials. Only the properties discussed further in the thesis are included. Second part of this chapter describes density functional theory simulations of structures of amorphous materials using the liquid-quench algorithm, and interpretation of bonding in obtained structures.

2.1 Methods used for synthesis and characterisation

2.1.1 Reactive magnetron sputtering of Si-B-C-N materials

Magnetron sputtering is one of Physical Vapour Deposition (PVD) techniques. It allows depositions of thin films of various materials by sputtering of elementary, alloy, compound or composite targets by positive ions in a plasmatic discharge. Sputtered particles together with particles of the discharge gas condense on opposite substrates and form the growing film. Magnetron placed below the sputtered target keeps free electrons in vicinity of the target, which increases degree of ionisation in the plasma and therefore increases efficiency of the sputtering. Structure and properties of the deposited films can be controlled mainly by composition of sputtered target, composition of the discharge gas mixture, substrate temperature and ions bombarding the growing film due to negative substrate bias.

![Diagram of the Balzers BAS 450 PM Cryo sputtering system used for depositions of Si-B-C-N materials.](image)

**Fig. 2.1:** The Balzers BAS 450 PM Cryo sputtering system used for depositions of Si-B-C-N materials. The discharge current on the magnetron target, $I_m$, was 1 A, and the negative substrate bias voltage, $U_b$, induced by the rf generator varied from -38 V to -700 V. The substrate temperature, $T_s$, was either maintained at 350 °C by an ohmic heater or allowed to equilibrate in the range 180 to 250 °C.
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Magnetron sputtering is one of the most versatile techniques compatible with semiconductor technologies and its further important advantage is an easy up-scaling. Contrary to some other techniques such as Chemical Vapour Deposition (CVD), it allows film generation at noticeably reduced substrate temperatures and without hydrogen-containing precursors resulting in an enlarged residual content of hydrogen in films.

For our experiments, we used a Balzers BAS 450 PM Cryo sputtering system with a planar rectangular unbalanced magnetron and a modified circular substrate holder (125 mm in diameter) – see Fig. 2.1. The Si–B–C–N films were deposited on p-type Si(100) substrates using dc magnetron co-sputtering of silicon, boron and carbon from high-purity composite targets (127×254×6 mm³). The targets used were C-Si-B: graphite overlapped by p-type Si and B stripes fixed to the target (see Fig. 2.2(a)), and B₄C-Si: boron carbide overlapped by p-type Si stripes (see Fig. 2.2(b)).

The Si fraction in the erosion target area was varied from 5 to 75 % for both targets, and the B fraction in the erosion target area was fixed at 20 % for the C-Si-B target. The total pressure of nitrogen-argon gas mixtures, p, was 0.5 Pa at the argon fraction in the gas mixture ranging from 0 to 75 % and at a constant gas flow approximately 25 sccm. The target-to-substrate distance was 100 mm. The discharge current on the magnetron target, I_m, was held constant at 1 A, and the negative substrate bias voltage, U_b, induced by an rf generator operating at a frequency of 13.56 MHz, was varied from a floating potential of approximately -38 V to -700 V. The substrate temperature, T_s, was adjusted at 350 °C by an ohmic heater or it was in the range from 180 to 250 °C without the heater. For comparison purposes, results on Si-B-C (100 % of Ar in the gas mixture) and B-C-N (0% of Si in the erosion area of the B₄C-Si target) materials are also included in this work.

Fig. 2.2: Geometric configuration of sputtered targets used for depositions of Si-B-C-N films: C-Si-B (a) and B₄C-Si (b).
2.1.2 Evaluating of discharge and deposition characteristics

The energy and total flux of ions bombarding the target and the growing films were evaluated on the basis of the discharge characteristics measured for both the dc magnetron discharge and the rf discharge dominating in the deposition zone. The discharge current on the magnetron target, $I_m$, and the corresponding cathode-anode voltage of the magnetron, $U_{dc}$, the time-averaged rf power, $P_{rf}$, absorbed by the plasma and the corresponding negative substrate bias voltage, $U_b$, relative to ground potential, were measured using respective units built into the dc and rf power supplies of the Balzers system. Only a slight effect (< 10%) of the non-ideal matching network on the $P_{rf}$ measurements under the given experimental conditions was proved by calorimetric tests after optimization of the electrical connection between the matching network and the substrate holder. Let us note that the measured $P_{dc}$ and $P_{rf}$ power values must be related to the magnetron erosion track area ($A_m = 140 \, \text{cm}^2$) and the area of the unshielded substrate holder ($A_s = 620 \, \text{cm}^2$), respectively, in order to obtain the respective power densities absorbed near the target and substrate. In addition, the value of pressure $p = 0.5 \, \text{Pa}$ was shown to be sufficiently low to ensure a collisionless motion of ions across the dc and rf sheaths under the conditions investigated.

Energy transfer and other processes affecting the energy balance in the low-pressure capacitive rf discharges were analyzed using the models given in Ref. 2. Such low-pressure discharges are strongly asymmetric due to a large difference between the area of the substrate holder $A_s = 620 \, \text{cm}^2$ and the total grounded area (10000 cm$^2$), leading to a high-voltage sheath near the powered substrate. The power balance equation can be then written as

$$P_{rf} = \Gamma_i A_s (E_i + E_c + E_e) \quad \text{(Eq. 2.1)},$$

where $\Gamma_i$ is the total time-average ion flux onto the substrate holder, $E_i$ is the mean kinetic energy transferred by an ion to the powered electrode, $E_c$ is the mean kinetic energy lost by an electron per electron-ion pair created in the gas mixture, and $E_e$ is the mean kinetic energy transferred by an electron to the grounded chamber walls. The $\Gamma_i$ values can be obtained from the $P_{rf}$ measurements if we take into account that for our high-voltage sheaths the effect of a low plasma potential $V_p$ can be neglected in the term for the mean ion kinetic energy $E_i = e(V_p - U_b)$ and that it can be put $E_c + E_e = 50 \, \text{eV}$ under a realistic assumption of a constant electron temperature $T_e = 3 \, \text{eV}$ in the substrate region. The ion energy per deposited atom, $E_{ia}$, was determined as

$$E_{ia} = e|U_b|\Gamma_i/\Gamma_p \quad \text{(Eq. 2.2)},$$

where the flux of film-forming particles onto the substrate, $\Gamma_p$, was calculated using a known atomic density of the films per unit area (determined by Rutherford back-scattering spectrometry) and a time of deposition.

2.1.3 Characterization of Si-B-C-N materials

The film thickness (up to 7 µm) and a bending of the substrate after deposition of the film, from which a residual macrostress was determined using the Stoney’s formula, were measured by profilometry (Dektak 8 Stylus Profiler, Veeco). Atomic force microscopy (Metris 2001A-NC Microscope, Burleigh Instruments) observation showed a very smooth surface morphology of the as-deposited layers with an average roughness $R_a \leq 0.8 \, \text{nm}$. X-ray diffraction analysis (Dron IV Diffractometer upgraded by Seifert GmbH) indicated their amorphous structure.

The elemental composition of the Si-B-C-N films (with small contents of Ar, H and O) was determined by Rutherford backscattering spectrometry (RBS) and elastic recoil
detection (ERD) methods using a Van de Graaf generator with a linear electrostatic accelerator. The contents of Ar, B, C, N, O and Si were measured by RBS using 2.390, 2.336 and 1.765 MeV (for carbon) protons as projectiles, scattered under the angle of 170°. The neutron depth profiling (NDP) was used to specify the boron content estimation when it was necessary. The content of H was measured by ERD with an incident beam of 2.75 MeV alpha particles at 75° to the sample surface normal. The hydrogen atoms recoiled under the angle of 30° were detected with a surface barrier detector covered by a 10 µm thick mylar stopping foil. The RBS and ERD measurements were evaluated by computer codes GISA and SIMNRA, respectively, using cross-section values from SigmaBase.

The chemical structure was analyzed by infrared variable angle spectroscopic ellipsometry (IR VASE). The IR VASE spectra were measured between 1.34 and 34 µm (i.e. approx. from 7000 to 220 cm⁻¹) using 3 angles of incidence 65, 70 and 75°, respectively. Similar to VIS VASE, these measurements were taken in reflection; therefore, the influence of substrate absorption, which is a critical factor in standard FTIR spectroscopy, was eliminated. Contrary to FTIR measurements, IR VASE (as ellipsometry in general) did not directly measure the absorption coefficient α, but it was determined from a simulation of the optical behavior in the IR region. The physical model used for IR VASE data consisted of a Si substrate with a native SiO₂ layer, a 'general oscillator' Si-B-C-N layer and a surface roughness layer. In the 'general oscillator' model, interband absorptions were simulated by Gaussian type oscillators; their parameters were found during a fitting procedure. Detected inhomogeneities were not larger than 10%.

Film hardness, effective Young’s modulus, E/(1 - ν²), where E and ν are the Young’s modulus and the Poisson’s ratio, respectively, and elastic recovery were determined using a computer-controlled microhardness tester (Fischerscope H-100B) which automatically records the depth of indentation of a Vickers diamond pyramidal tip, while increasing the applied load up to a preset maximum. The plastic hardness was calculated from the indentation depth after unloading, and it was corrected for the indentation size effect. To obtain reliable hardness values of the films (see, for example, Ref. 8), measurements were performed with a maximum load of 30 and 50 mN.

Resistivity of selected Si-B-C-N samples, deposited on non-conductive glass substrates, was measured by the four points technique (with 1.047 mm spacing between tips).

2.2 Methods used for atomistic simulations

2.2.1 Ab-initio simulations

Levels of simplification used in molecular and material simulations include (starting with the most exact ones) quantum chemical methods, density functional theory, environment-dependent interaction potentials-based methods, tight binding methods and empirical potentials-based methods. Detailed overview of them together with comparing of simulation results can be found in Ref. 9. First two of listed methods are ab initio – that is, they do not include any empirical fitting parameters. All calculations reported in this work use the density functional theory (DFT) which is based on the following theorems and simplifications:

(1) Instead of the (relativistic) Dirac equation the (unrelativistic) Schrödinger equation can be used for light atoms where the relativistic effects are negligible.
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(2) The many-electron problem can be transposed to many one-electron equations (Schrödinger-type) coupled by an effective potential given by the electron charge density \( n(\mathbf{r}) \). It holds

\[
n(\mathbf{r}) \geq 0 \quad \text{and} \quad \int n(\mathbf{r}) d\mathbf{r} = N
\]  
(Eq. 2.3, 2.4)

where \( N \) is a total number of electrons.

(3) The total energy \( E[n(\mathbf{r})] \) can be minimized so

\[
E[n(\mathbf{r})] \geq E[n_0] = E_0
\]
(Eq. 2.5).

(4) It holds (Hohenberg and Kohn)

\[
E[n(\mathbf{r})] = \int v(\mathbf{r}) n(\mathbf{r}) d\mathbf{r} + F[n(\mathbf{r})]
\]
(Eq. 2.6)

where \( v(\mathbf{r}) \) is an external potential (due to the ions) and \( F[n(\mathbf{r})] \) is universal functional valid for any \( v(\mathbf{r}) \):

\[
F[n(\mathbf{r})] = 1/2 \int\int n(\mathbf{r}) n(\mathbf{r}') / |\mathbf{r} - \mathbf{r}'| d\mathbf{r} d\mathbf{r}' + T[n(\mathbf{r})] + E_{xc}[n(\mathbf{r})]
\]
(Eq. 2.7).

The first term accounts for the long-range Coulomb interaction and \( T[n(\mathbf{r})] \) is the kinetic energy of electrons. The exchange and correlation energy \( E_{xc} \) accounts for the antisymmetric nature of any true many-electron wavefunction with respect to exchange of spin and space coordinates of any pair of electrons, and for self-interaction of the electron with itself (which would be otherwise included in the calculation).

(5) The system of the one-electron Schrödinger-like equations (Kohn-Sham equations) can be then written as

\[
(-\frac{1}{2} \nabla^2 + v(\mathbf{r}) + \int n(\mathbf{r}') / |\mathbf{r} - \mathbf{r}'| d\mathbf{r}' + \mu_{xc}[n(\mathbf{r})]) \psi_i = \varepsilon_i \psi_i
\]  
(Eq. 2.8)

where

\[
\mu_{xc}[n(\mathbf{r})] = \frac{\partial E_{xc}[n(\mathbf{r})]}{\partial n(\mathbf{r})}
\]  
(Eq. 2.9).

In general case, the Lagrange parameters \( \varepsilon_i \) have not any physical meaning (the only aim is to calculate the wavefunction).

(6) Classes of methods treating the exchange and correlation potential \( \mu_{xc} \) include the local density approximation (LDA) where only dependence on local electron charge density is considered:

\[
\mu_{xc}[n(\mathbf{r})] \approx \mu_{xc}^{\text{LDA}}[n(\mathbf{r})]
\]  
(Eq. 2.10),

the local spin density approximation (LSD) where the spin effects are incorporated:

\[
\mu_{xc}[n(\mathbf{r})] \approx \mu_{xc}^{\text{LSD}}[n^+(\mathbf{r}), n^-(\mathbf{r})]
\]  
(Eq. 2.11),

and the generalised gradient approximation (GGA) which incorporates also the non-local contributions:

\[
\mu_{xc}[n(\mathbf{r})] \approx \mu_{xc}^{\text{GGA}}[n(\mathbf{r}), \nabla n(\mathbf{r})]
\]  
(Eq. 2.12).

The ab initio molecular dynamics (MD) method integrates the classical equations of motion for the nuclei and thereby provides insights into the time-evolution of the system. For simulations of our materials we employed the DFT as implemented in the Car-Parrinello Molecular Dynamics (CPMD) software. This particular implementation used has the following features:
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(1) Atom cores and the core electrons are represented using pseudopotentials. A pseudopotential is a potential that gives rise to wavefunctions identical in shape with those of true valence wavefunctions outside the core region, but without nodes inside the core region. Such pseudo-wavefunctions can be accurately represented with far fewer plane waves than are required to represent the true valence wavefunction\(^\text{13}\). For our calculations we used the Goedecker-type pseudopotentials\(^\text{14}\).

(2) The Kohn-Sham equations for the valence electrons are expanded in a basis of plane wave functions; in our case with an energy cut-off of 60 Ry. This value was found to be sufficient to reproduce measured data for a number of related molecular structures (see below). Exchange and correlation terms were treated in the generalised gradient approximation (GGA) using the BLYP functional\(^\text{15,16}\).

(3) The electronic problem is solved in parallel with motion of nuclei (positive ions) by introducing a fictitious classical dynamics for electrons. Instead of optimizing wavefunction after each ionic step, in the same time step the ions are moved according to the self-consistent forces, while the electronic variables are moved according to the electronic gradients and constraints. All MD runs were performed using an as long as possible time step of 0.073 fs (3 atomic units, the calculations were becoming unstable for time steps $\geq$ 4 atomic units). The fictitious electron mass (required for the classical integration of the electronic degrees of freedom) was set to 200 me.

(4) Calculations were performed in a three-dimensionally periodic cubic cell at the gamma-point only - in other words, terms in the wavefunctions with wavelengths longer than the cell size were not considered. This is well possible for disordered systems where we expect the orbitals to be relatively localised\(^\text{13}\).

The accuracy of this method as well as the convergence of calculated properties with respect to plane-wave cut-off was confirmed using simulations of 8 representative molecules ($\text{B}_3\text{N}_3\text{H}_6$, silacyclobutane $\text{SiC}_3\text{H}_6$, trimethylborane $\text{B(CH}_3)_3$, pyrrole $\text{NC}_4\text{H}_5$, pyrazine $\text{N}_2\text{C}_4\text{H}_4$, silyl cyanide $\text{SiCNH}_3$, ($\text{SiH}_3$)$\text{NCN}$ and trimethylamineborane ($\text{CH}_3$)$_3\text{NBH}_3$). Calculated energies were within 1 % of the asymptotic value for large plane wave cut-off. Typical differences after geometry optimisations between the experimental and simulated bond lengths and angles were only 1-2 %, with convergence for N and B slightly worse than for Si, C and H. Fig. 2.3 shows geometry optimization results for the $\text{B}_3\text{N}_3\text{H}_6$ molecule.

2.2.2 The liquid-quench algorithm

Amorphous (Si)-(B)-C-N materials were studied by molecular dynamics simulations using a liquid-quench algorithm. This algorithm attempts to capture the formation conditions of the real materials, which arise from rapid cooling of the localized melt (thermal spike) created around sites of energetic ion impact.

It is not possible using presently available quantum theoretical methods to simulate the full ion bombardment process. We simplify the process by assuming that the primary impact creates a localized region of high temperature, commonly referred to as a thermal spike. Thermal spikes have a cooling time sufficiently short to be simulated using ab initio MD methods as shown in Ref. 17. These cooling times can be estimated using the heat diffusion equation together with literature values for the thermal diffusivity and the thermal spike radius\(^\text{17}\). The thermal spike simulation method has been used successfully to predict the structure of carbon materials formed from ion beams having a range of energies\(^\text{18}\). Our liquid quench simulations were performed in a number of stages:
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(1) **Start-up:** Alternately distributing of atoms of all types over the simulation cell (most typically using a simple tetragonal structure – e.g. four $5 \times 5$ planes for 100 atoms) followed by a random shift of atoms (with an amplitude of 1 Å) generated a semi-random initial start-up structure.

(2) **Initial Mixing:** In order to obtain a completely randomized structure with no memory of the initial structure, an MD run of 1 ps length at a temperature of at least 5000 K (Nose-Hoover thermostat) was carried out. The mixing was considered to be sufficient when the square root of the mean squared displacement (MSD) was longer than half of the cell size as described previously. A significantly reduced plane-wave cut-off of 10 Ry was adopted for this stage of the simulation only. High accuracy of the DFT energies is not required for this stage and cut-off reduction increases the efficiency of this stage of the simulation dramatically. Low cut-off was also found useful since it effectively prevents the formation of stable bonds, which would interfere with efficient mixing.

(3) **Exponential Cooling:** After wavefunction optimisation, the material was exponentially cooled to its (rounded) deposition temperature of 650 K. Temperature control was achieved by velocity scaling of ions when actual and target temperature differed by more than 10%. Various cooling times were used in the simulations.

(4) **Equilibration:** After the cooling phase, sample equilibration was accomplished using a 1 ps MD run at 650 K (Nose-Hoover thermostat). The purpose of equilibration is for the system to fully recover thermal equilibrium as indicated by a constant mean squared displacement.

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**Fig. 2.3:** Results after optimizing of geometry of $B_3N_3H_6$ molecule at various energy cutoffs. Panel (a) shows convergence of selected geometric quantities. Panel (b) shows convergence of total energy and an averaged time needed for one optimization step. Molecule was placed in 12 Å cubic cell with periodic boundary conditions applied.
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(5) Production Run: Following equilibration, various quantities of interest (bonding statistics, Kohn-Sham energies and stresses) were computed as statistical averages over at least 0.5 ps long MD run at 650 K.

(6) Post-processing: The stable structure obtained at the end of the liquid quench algorithm is wavefunction optimised at two cut-offs above and below 60 Ry in order to estimate the Pulay correction of the averaged stress. Same structure was used as a basis of calculations of other properties of interest (such as thermal stability or optical conductivity) described in detail in respective chapters.

2.2.3 Bonding analysis

Our bonding analysis is based on representation of valence electrons by maximally localized Wannier function centres (WFC). In this concept, the Bloch states are expressed as a sum of orthogonal functions \( w_n \) with their total spread - for n-th function

\[
\sigma_n = \sqrt{\langle r^2 \rangle_n - \langle r \rangle_n^2}
\]

(Eq. 2.13)

- minimized in the space. To simplify the analysis, rather than visualize the spatial structure of maximally localized Wannier functions, only the coordinates of Wannier function centers are calculated as

![Fig. 2.4: Pair correlation functions of Si, B, C and N atoms with nearby Wannier function centres for Si-B-C-N sample of composition Si\(_{14}\)B\(_{23}\)C\(_6\)N\(_{55}\). The arrows denote suitable positions of distance cutoffs.](image-url)
\[ x_n = -\frac{L}{2\pi} \text{Im} \ln \left| \frac{e^{-\frac{2\pi}{L} \lambda_n}}{w_n} \right| \]  
(Eq. 2.14)

(and similarly for \( y_n, z_n \)), where \( L \) is the periodical cell size.

For our structures, we calculate the pair correlation functions of Si, B, C and N atoms with nearby WFCs. The first minimum in these pair functions defines a distance cut-off for each atom type as shown in Fig. 2.4. This gives for each WFC a set of associated atoms located within the cut-off for that atom type. If the set contains only one atom, the WFC is classified as a lone-pair. If the set contains two atoms, the WFC is classified as a bonding electron pair representing a bond between these two atoms. Multiple bonds are characterised by multiple WFCs between the same two atoms. Three centre, two electron bonds are characterised by a WFC associated with three atoms. We ascribe strength 0.5 to the bonds arising from this electron pair between the closest atom to the WFC and the two others. The bond strength between any two atoms is obtained by summing the contributions from all WFCs associated with that pair. This interpretation ensures that the sum of strengths of all bonds is equal to the number of bonding electron pairs in the network. For purposes where matters only an existence or non-existence of a bond (such as calculating of network rings), any pair of atoms linked with bond strength \( \geq 0.5 \) was considered as bonded.

2.3 References

3 Influence of target and gas composition on structure and properties of Si-B-C-N films

This chapter is based on part of results published in Refs. 1 and 2, while summary of all achievements is provided in the first chapter (section 1.2.1).

As a result of short chemical bonds with low polarities and high average coordination numbers of elements, compounds within the Si–B–C–N system can form superhard materials (see, for example, Refs. 3 and 4). We systematically investigated reactive dc magnetron sputtering of Si–B–C–N films using a composite C–Si–B target in nitrogen-argon gas mixtures. The main aim of our work was to develop a reproducible process for the formation of hard Si–B–C–N films with a high oxidation resistance at elevated temperatures, low internal stresses and good adhesion to various substrates. In this chapter, we report on the effect of Si fraction in the C–Si–B target and the effect of the N₂–Ar gas mixture composition on the elemental composition, bonding structure and mechanical properties of the films prepared at a range of negative substrate biases and substrate temperatures (≤ 350 °C). Furthermore, we report on the effect of Si content in Si-B-C-N films on compressive stress generated in the films by implanted Ar atoms.

3.1 Experimental conditions

The effect of the C–Si–B target composition on characteristics of the Si–B–C–N films (Figs. 3.3–3.5) is presented for a fixed 20 % boron fraction in the erosion area of the target, a 50 % N₂ + 50 % Ar gas mixture and two different choices of the U_b and T_s values. In case of U_b = -500 V and T_s = 350 °C we were interested in examining the effect of ion bombardment and high substrate temperature simultaneously during film growth. In the second set of experimental conditions no rf-induced substrate bias was applied or ohmic heater used. In this case the substrate was at floating potential, U_s = U_f = -15 to -38 V, with a temperature of T_s = 180–190 °C.

The effect of the N₂–Ar gas mixture composition characteristics of the Si–B–C–N films (Figs. 3.6-3.8) is presented for a fixed composition (60 % Si +20 % B+20 % C) in the erosion target area, with T_s = 350 °C and two different values of U_b = -100 and -500 V.

In order to examine compressive stress as a function of Si and Ar content, a set of 30 samples was prepared by combining six different B₄C-Si target compositions with five different deposition conditions (gas composition, substrate bias and temperature). The six target compositions were Siₓ(B₄C)₁₀₀-x with x=0, 5, 20, 40, 60, 75. The five depositions conditions were: (1) 50% Ar + 50% N₂ gas mixture and substrate temperature of 350 °C with U_b = -100 V; (2) Same with U_b = -500V; (3) 75% Ar + 25% N₂ gas mixture with U_b = -100 V and substrate temperature of 700 °C; (4) same with substrate temperature of below 180-190 °C (no ohmic heating) and (5) discharge gas of 100% Ar with U_b = -100V and substrate temperature of 350 °C. Compressive stresses and elemental compositions were measured for all thirty samples.
3.2 Specification of hardness measurements

Hardness (and the other mechanical properties) of the films was determined using the Fischerscope H-100B microhardness tester (see chapter 2). For each selected maximal load of the diamond tip, the loading-unloading indentation curves were measured for at least 27 points, with loading and unloading times (60 s) sufficiently high to obtain values independent of these times. An example of the averaged loading-unloading curve is given in figure 3.1. A tangent line was made using the top 30% of the averaged unloading curve, and the "corrected depth" $h_r$, defined by the point of intersection of the tangent with the indentation depth axis, was evaluated. The plastic hardness was then calculated as

$$H_{plast} = \frac{L}{26.43h_r^2} \quad \text{(Eq. 3.1)},$$

where $L$ is the maximal load and $26.43h_r^2$ is a contact area of the Vickers diamond tip with a sample at indentation depth $h_r$.

**Fig. 3.1:** Average over loading-unloading indentation curves measured on a typical Si-B-C-N sample (copied from the screen of the Fischerscope H-100B microhardness tester). The line is a tangent made using top 30% of the unloading part of the curve. The calculated quantities $W_t$, $W_e$, $W_r$, $E/(1-\nu^2)$, $H_{plast}$ and $h_r$ are total, elastic and plastic work of the indentor, modified Young’s modulus, plastic hardness and depth defined by the point of intersection of the tangent with the indentation depth axis, respectively.
Note that measured values of hardness depend on the load used because (1) at low loads the hardness value cannot be determined with precision owing to the large elastic recovery, dominating the load-unload curves, while (2) at high loads, leading to maximal indentation depths over 5-10% of the sample thickness, the evaluated hardness may be underestimated due to the effect of the softer substrate. Figure 3.2 shows dependence of hardness on the load used for a typical Si-B-C-N sample. Sample thickness was 7.2 μm, and the maximal indentation depth was less than 10% of the thickness for all loads shown.

![Graph showing hardness vs maximal load](image)

Fig. 3.2: Dependence of measured plastic hardness on maximal load for a typical Si-B-C-N sample. Sample thickness was 7.2 μm, and the maximal indentation depth was less than 10% of the thickness for all loads shown.

Note that measured values of hardness depend on the load used because (1) at low loads the hardness value cannot be determined with precision owing to the large elastic recovery, dominating the load-unload curves, while (2) at high loads, leading to maximal indentation depths over 5-10% of the sample thickness, the evaluated hardness may be underestimated due to the effect of the softer substrate. Figure 3.2 shows dependence of hardness on the load used for a Si-B-C-N sample of exceptionally high thickness of 7.2 μm, where the indentation depths were less than 10% of 7.2 μm for all loads up to 100 mN. It can be seen that the measured values are overestimated for loads up to 30 mN. However, at a higher load of 50 mN the indentation depths were already too high (occasionally over 30% of the film thickness) for most of the Si-B-C-N samples studied in chapters 3 and 4 (film thickness starting at 1.0 μm). The hardness values are therefore presented at the both loads of 30 and 50 mN, which best fulfils the conditions mentioned above.
3.3 Results

3.3.1 Effect of the magnetron target composition

In Fig. 3.3(a) it is shown that the increasing silicon fraction in the erosion target area results in a rising incorporation of silicon (from 10 to 29 at. % for \( U_b = -500 \) V and \( T_s = 350 \) °C, and from 8 to 30 at. % for \( U_s = U_f = -15 \) to \(-38 \) V and \( T_s = 180–190 \) °C) and nitrogen (from 32 to 46 at. % and from 36 to 50 at. %, respectively) into the films, while the carbon content decreases (from 35 to 5 at. % and from 40 to 2 at. %, respectively) with a slowly decreasing boron content (from 12 to 7 at. %) for \( U_b = -500 \) V and \( T_s = 350 \) °C, and practically constant boron content (from 10 to 8 at. %) for \( U_s = U_f = -15 \) to \(-38 \) V and \( T_s = 180–190 \) °C. The incorporation of Si raises the N content in the layers apparently due to preferred formation of Si–N bonds.\(^6,7\) In addition, the substantially lower values obtained for the C content in the films prepared with high substrate bias and temperature (\( U_b = -500 \) V and \( T_s = 350 \) °C) can be mainly explained by a strong ion-induced and thermal desorption of loosely bonded C–N species from the surface of growing films\(^8\) (as indicated by decrease of the deposition rates under these conditions - Ref. 1).

Figure 3.3(b) provides information on the content of hydrogen, oxygen and argon in the Si–B–C–N films. The hydrogen content is in the range from 5 to 9 at. % for samples...
deposited with high substrate bias compared to 4-6 at. % for low bias conditions. The oxygen content (3–5 at. %) is also greater in the case of high applied bias. This may be due to subplantation of hydrogen and oxygen atoms into the films from the discharge plasma. A maximum value (9 at. %) determined for a residual content of hydrogen in our films is still considerably lower than the usual values (approximately 15 at. %) reported in the literature \(^6, ^9\) for Si–B–C–N films prepared by plasma-assisted chemical vapor deposition using H-containing precursors at reduced substrate temperatures. An increasing subplantation of argon into the films (up to 3 at. %) with the silicon fraction in the erosion target area \([\text{Fig. 3.3(b)}]\) has been correlated with stronger ion bombardment (higher \(\Gamma_i/\Gamma_p\) ions to film-forming particles flux ratio) \(^1\). The higher \(\Gamma_i/\Gamma_p\) flux ratio at higher silicon fraction in the erosion target area is caused by an increasing plasma conductivity due to a higher secondary electronic emission coefficient and sputtering yield of silicon compared with carbon \(^{10}\).

Information about the chemical structure was obtained from IR VASE measurements. Figure 3.4 shows that for the highest Si, the dominant absorption peak is due to a presence of Si-N bond (960 cm\(^{-1}\))\(^{11}\). This peak decreases as the silicon fraction decreases and characteristic peaks due to the presence of C-C (1360-1580 cm\(^{-1}\))\(^{11}\), C=C (1600-1630 cm\(^{-1}\))\(^{12}\), C(sp\(^3\))-N (1300 cm\(^{-1}\))\(^{12}\) and C(sp\(^2\))-N (1600 cm\(^{-1}\))\(^{11}\) bonds increase. In addition, the peak of B(sp\(^3\))-N (1385 cm\(^{-1}\))\(^{13}\) bond was identified. In the region around 1100 cm\(^{-1}\) possible contributions to the absorption coefficient could arise from an asymmetric vibration due to the Si-O (1090-1110 cm\(^{-1}\))\(^{14}\) bond, absorption due to the B-C (1100 cm\(^{-1}\))\(^{13, 15}\) bond and/or the B(sp\(^3\))-N (1060-1100 cm\(^{-1}\))\(^{13}\) bond. The freestanding peak in the region of high energies could arise from the presence of C(sp)-N (2200 cm\(^{-1}\))\(^{11}\) and/or Si-H (2100 cm\(^{-1}\))\(^{14}\) bonds. The absorption peak due to the Si-N bond in the low energy region is likely to be broadened due to

**Fig. 3.4:** The dependence of the absorption coefficient on wavelength in the infrared region, obtained by IR VASE for films prepared in a 50 % N\(_2\) + 50 % Ar gas mixture at various silicon fractions in the erosion target area (corresponding to the 5-75% Si labels on the curves) for \(U_b = -500 \text{ V}\) and \(T_s = 350 \degree \text{ C}\) (solid lines), and \(U_s = U_f = -15\) to -38 V and \(T_s = 180-190 \degree \text{ C}\) (dashed lines).
the combination of absorptions from Si-C (780 cm\(^{-1}\))\(^{11}\), B(sp\(^2\))-N (780 cm\(^{-1}\))\(^{15}\) and a number of other bonds which have not been marked on the Figure 3.4, including vibrations of Si-Si bonds in the substrate at 610 cm\(^{-1}\), deformation of B-O-Si bonds at 670 cm\(^{-1}\), bending of B-O-B bonds at 720 cm\(^{-1}\), bending of Si-O-Si bonds at 810 cm\(^{-1}\), stretching of B-O-Si bonds at 930 cm\(^{-1}\) and vibrations of a B-B network at 942 cm\(^{-1}\)\(^{16,17}\).

Figure 3.5 presents the results obtained for hardness, effective Young’s modulus and elastic recovery of the films. The figure shows that the replacement of carbon by silicon in the films has significantly different effects depending on the substrate bias and temperatures used in the deposition process. The values of hardness (24–27 GPa), effective Young’s modulus (170–180 GPa) and elastic recovery (72–73 %) for films made with \(U_b = -500\) V and \(T_s = 350\) °C are not substantially affected by the replacement of carbon by silicon. In contrast, replacement of carbon by silicon is accompanied by a strong increase in hardness (from 17 to 33 GPa with a maximum load of 30 mN), effective Young’s modulus (from 135 to 216 GPa) and a slower rise in elastic recovery (from 65 to 73 %) for samples made with \(U_s = U_f = -15\) to -38 V and \(T_s = 180–190\) °C.

As can be seen in Fig. 3.5(a), ion bombardment effects and thermal desorption lead to an enhanced hardness of the films with high carbon content. This is believed to be due to the

**Fig. 3.5:** Hardness measured with the presented maximum load (a), and effective Young’s modulus, \(E/(1 - \nu^2)\), and elastic recovery measured with a maximum load of 30 mN (b) for films prepared in a 50 % N\(_2\) + 50 % Ar gas mixture at various silicon fractions in the erosion target area for \(U_b = -500\) V and \(T_s = 350\) °C (full symbols), and \(U_s = U_f = -15\) to -38 V and \(T_s = 180 - 190\) °C (empty symbols).
removal of volatile C–N compounds from the growing film surface. In contrast, for films with high silicon content conditions of energetic ion bombardment and elevated temperature cause a lower hardness. The ion kinetic energy may be too high to form an optimized superhard densified structure of the deposited material with highly coordinated B(sp$^3$)–N and C(sp$^3$)–N bonds.

3.3.2 **Effect of the gas composition**

As can be seen in Fig. 3.6(a), the Si content in the films increases (from 23 to 30 at. % for $U_b = -500$ V and from 24 to 29 at. % for $U_b = -100$ V) with increasing argon fraction in the gas mixture due to the enhanced physical sputtering of silicon from the composite target. A chemical affinity for nitrogen of silicon in the deposited material leads to an only a weak decrease (from 53 to 44 at. % for $U_b = -500$ V and from 51 to 44 at. % for $U_b = -100$ V) in the N content in the films in spite of the substantial decrease (4 times) in the N$_2$ partial pressure in the discharge gas. The content of boron in the films is practically constant (7–8 at. %) for $U_b = -500$ V and slowly decreases (from 11 to 6 at. %) for $U_b = -100$ V, while that of carbon is in the range from 5 to 9 at. % and 5 to 13 at. %, respectively. Much stronger ion-induced effects at $U_b = -500$ V result in a systematically lower (typically by 2 at. %) incorporation of both these elements into the films except for boron at a 75 % Ar fraction in the gas mixture when a dynamic balance determining the film composition was noticeably changed [see the enlarged C content and Fig. 3.6(b)].

![Fig. 3.6: Elemental composition of films prepared at various argon fractions in the gas mixture, a fixed 60 % Si + 20 % B + 20 % C erosion target area and $T_s = 350$ °C for $U_b = -500$ V (full symbols) and $U_b = -100$ V (empty symbols).]
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Fig. 3.6(b) shows the incorporation of argon and residual gas elements in the films. It appears that an intensified bombardment of the growing films by Ar\(^+\) ions leads to subplantation of argon atoms into the films (up to 6 at. % for \(U_b = -500\) V and 2 at. % for \(U_b = -100\) V). As a result of the stronger bombardment by argon ions which leads to much higher deposition rates, the volume concentrations of hydrogen and oxygen in the films decrease to only 2 at. % for both the \(U_b\) values and at the 75 % Ar fraction in the discharge gas.

Figure 3.7 shows the influence of the \(N_2\)-Ar gas composition on the chemical bonding in the Si-B-C-N films as measured by IR VASE. There is a strong increase in the Si-N absorption as a natural consequence of increasing Si content in films (see Fig. 3.6). The affinity of Si for N leads to an increase in the number of Si-N bonds in spite of a reduction in the N content in the gas. The decreased N content reduces the number of C(sp\(^3\))-N, B(sp\(^2\))-N and C(sp)-N bonds, which may be responsible for hardness increase [see Fig. 3.8(a)]. In the case of 75 % Ar in the gas mixture it appears only absorption peak due to a presence of Si-N bond and its tail in the range of 1100-1300 cm\(^{-1}\). Although exact positions of local maxima in the spectra may be affected by the shoulder of the dominant Si-N peak, in these compositions the tail most likely corresponds to bonds with C(sp\(^3\)) and B(sp\(^2\)). Absorption due to presence of bonds of C with C and N in the range of 1500-1600 cm\(^{-1}\) is much stronger in case of deposition with low Ar concentration in the gas mixture for \(U_b = -100\) V as compared to \(U_b = -500\) V. We believe that this is caused by lower desorption of volatile C-N compounds from the growing film surface\(^8\) at lower biases (see twice higher C concentration in films in Fig. 3.6).

\[\text{Fig. 3.7: The dependence of the absorption coefficient on wavelength in the infrared region, obtained by IR VASE for films prepared at various argon fractions in the gas mixture (corresponding to the 0-75 % Ar labels on the curves), a fixed 60 % Si + 20 % B + 20 % C erosion target area and } T_s = 350 \degree C \text{ for } U = -500 \text{ V (solid lines) and } U = -100 \text{ V (dashed lines).}\]
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There is a stronger absorption peak corresponding to the B(sp\textsuperscript{2})-N bond at 1385 cm\textsuperscript{-1} for \(U_b = -100\) V than for \(U_b = -500\) V in the case of both 0 and 25 % Ar concentration in the gas mixture. This shows that B has a similar behavior to C in that it is preferentially removed from the growing film under high bias conditions (see higher B and C concentrations in films for lower bias voltage in Fig. 3.6).

In the case of 75 % Ar in the gas mixture there is a difference in the level B and C incorporation into films due to the increased Si content (see surprising increase of C content in films for both \(U_b = -100\) V and \(U_b = -500\) V). The silicon preferentially bonds to the carbon because of the stronger Si-C bond compared to the Si-B bond\textsuperscript{16}.

Figure 3.8 shows that an increasing argon fraction in the gas mixture leads to a progressive rise in hardness, effective Young’s modulus, \(E/(1 - \nu^2)\), and elastic recovery measured with a maximum load of 30 mN (b) for films prepared at various argon fractions in the gas mixture, a fixed 60 % Si + 20 % B + 20 % C erosion target area and \(T_s = 350\) °C for \(U_b = -500\) V (full symbols) and \(U_b = -100\) V (empty symbols).

**Fig. 3.8:** Hardness measured with the presented maximum load (a), and effective Young’s modulus, \(E/(1 - \nu^2)\), and elastic recovery measured with a maximum load of 30 mN (b) for films prepared at various argon fractions in the gas mixture, a fixed 60 % Si + 20 % B + 20 % C erosion target area and \(T_s = 350\) °C for \(U_b = -500\) V (full symbols) and \(U_b = -100\) V (empty symbols).

Figure 3.8 shows that an increasing argon fraction in the gas mixture leads to a progressive rise in hardness, effective Young’s modulus and elastic recovery of the films for both the \(U_b\) values considered. However, the values obtained for these quantities at \(U_b = -100\) V are systematically higher (hardness up to 47 GPa, the effective Young’s modulus up to 290 GPa and the elastic recovery up to 88 % measured with a maximum load of 30 mN).
Taking into account the respective increase in the fraction of \( \text{Ar}^+ \) ions in the total ion flux onto growing films at a fixed \( U_b \) value, the rising film hardness (and hence the effective Young’s modulus) can be explained by ion-induced knock-on subplantation of film-forming particles and by direct subplantation of argon into the films [see Fig. 3.6(b)], which results in densification of the deposited materials\(^{20,21}\). In previous work on sputter-deposited C–N\(^8,22\) and Si–C–N\(^23\) films indicated that increased hardness was correlated with enhanced ion-induced desorption of loosely bonded C–N species from the surface of growing films and with a decreased residual concentration of hydrogen [see Fig. 3.6(b)]. In the case of our amorphous Si–B–C–N materials the formation of hard, densified (density around 2.4 g cm\(^{-3}\)) films correlated with the use of the negative substrate bias voltage \( U_b = -100 \) V with the corresponding low values of the \( \Gamma_i/\Gamma_p \) flux ratio were found to be almost optimum for formation of hard densified amorphous Si–B–C–N materials (density around 2.4 g cm\(^{-3}\)) with strong local covalent bonds under the experimental conditions investigated\(^{18}\). Detailed discussion of the effect of substrate bias on film characteristics is given in the chapter 4.

**Fig. 3.9**: Experimental compressive stresses in Si-B-C-N films as a function Ar and Si content. The figure shows that the linear dependence of stress and Ar content decreases with an increase in the Si content. Samples are prepared as described in the text. Not shown are the results for samples with 60 and 75 % Si content in the B\(_4\)C target, which, like the 40 % samples, did not exhibit any correlation of stress and Ar content.
3.3.3 Effect of Si- and Ar-content on compressive stress

Figure 3.9 shows the compressive stress measured in the Si-B-C-N samples as a function of Si and Ar content. We note that the elemental analysis confirmed that the percentage of Si in the films increases with the ratio of Si in the sputtered target (see Fig. 3.3). The results show that for samples with low Si content, there exists a linear dependence between the amount of implanted Ar and the compressive stress in the films. For the samples with higher Si content, the correlation between Ar content and compressive stress is less clear. In case of the 20% Si targets there appears to be a weak correlation while there is no observable dependence for the 40, 60 and 75% Si targets. Collectively, the data shows that an increase in Si content results in a decrease in the dependence of compressive stress on Ar content. These results suggest that implanted Ar is a source of compressive stress in Si-B-C-N films with low Si content, while in high Si content samples, stress generation through implanted Ar appears to be inhibited. The phenomena shown are discussed in detail by means of computer simulations in chapter 7.

It is postulated that the low values (close to 1 GPa) of compressive stress in the films deposited with high silicon content and low $\Gamma_i/\Gamma_p$ values\(^{18}\) are due to the ability of silicon to form very easy distorted bonds with minimal energy penalty and the relatively low levels of ion bombardment during growth in agreement with Ref. 9. In addition, practically no correlation between the compressive stress and film hardness was observed except for the films prepared in a 25% N\(_2\) + 75% Ar gas mixture, for which a slightly higher compressive stress rising from 1.2 GPa (U\(_b\) = -500 V) to 1.6 GPa (U\(_b\) = -100 V) was obtained in a qualitative agreement with theoretical predictions\(^{18,20,24}\).

3.4 Conclusions

Reactive dc magnetron co-sputtering using a composite C–Si–B target in a nitrogen-argon gas mixture at substrate temperatures of 180–350 °C has proved to be a suitable technique for the deposition of new quaternary Si–B–C–N materials with outstanding physical properties. In particular, the Si–B–C–N films deposited in this way exhibit high hardness (up to 47 GPa) and elastic recovery (up to 88 %) at a low compressive stress (1.0–1.6 GPa).

Our results suggest that not only the composition of the C–Si–B target and the N\(_2\)–Ar gas mixture, but also substrate bias-related ion bombardment characteristics (particularly ion kinetic energy and ion-to-film-forming particles flux ratio) are important deposition parameters making it possible to control elemental composition, chemical bonding and the properties of the films formed over a wide range. These phenomena are discussed further in chapter 4 where the effect of bias is explored in detail.

Most significant chemical bonds in materials were found to be bonds of Si, B and C with N [Si-N, B(sp\(^{2-3}\))]-N and C(sp\(^{1-3}\))-N in all compositions studied, and C=C and C=C bonds mainly at high carbon content, at a presence of Si–C, Si–O and Si–H bonds.

We have shown a correlation of stress in Si-B-C-N films prepared by sputtering in nitrogen-argon mixture with the content of argon in the film. The strength of the correlation decreases steadily with increasing silicon content. This suggests the ability of silicon to relieve compressive stress, generated by implanted argon, in the Si-B-C-N films.


3.5 References

Chapter 4 - Influence of substrate bias voltage

4 Influence of substrate bias voltage on structure and properties of Si-B-C-N films prepared by reactive magnetron sputtering

This chapter is based on results published in Ref. 1. It reports on the effect of the rf induced negative substrate bias voltage, $U_b$, on characteristics of the Si-B-C-N films (elemental composition, surface bonding structure, and mechanical and electrical properties) at several sputtered target and gas mixture compositions (selected on the basis of results included in the previous chapter).

In this chapter we systematically study the influence of an rf induced negative substrate bias on the reactive dc magnetron deposition of Si-B-C-N films using a co-sputtering of silicon, boron and carbon from a single composite target in nitrogen-argon gas mixtures. The influence of the C-Si-B target composition and the discharge gas mixture on the structure and mechanical properties of the films were investigated in the previous chapter. The films were found to be amorphous with a very smooth surface ($R_a \leq 0.8\,\text{nm}$) and good adhesion to substrates with a low compressive stress (1.0 - 1.6 GPa). They exhibited high hardness (up to 47 GPa) and high elastic recovery (up to 88%). They also found to have extremely high oxidation resistance in air at elevated temperatures (up to 1350 °C – the limit imposed by the substrate). Here we report on the effect of the negative substrate bias voltage on the discharge and deposition characteristics, and on elemental composition, surface bonding structure, and mechanical and electrical properties of the films prepared using C-Si-B and B$_4$C-Si composite targets at various substrate temperatures ($\leq 350\,\text{°C}$). In addition, the low values of the internal stresses generated in the films will be presented and discussed.

4.1 Experimental conditions

The effect of the negative substrate bias voltage on the discharge and deposition characteristics, and on characteristics of the Si-B-C-N films is presented for films deposited using two different composite sputtering targets (C-Si-B sputter target with fixed 20% C + 60% Si + 20% B erosion area and B$_4$C-Si target with a fixed 40% B$_4$C + 60% Si erosion area). The two different composite targets with the same 60% Si fraction in the erosion area were used at a fixed 25% N$_2$ + 75% Ar gas mixture and $T_s = 350\,\text{°C}$ to investigate the influence of the changed target composition leading to noticeably different boron and carbon contents in films (Figs. 4.2, 4.4 and 4.7).

Two different substrate temperatures, $T_s = 180$-250 °C and $T_s = 350$ °C, were used to investigate the role played by thermally activated processes during film growth in a 50% N$_2$ + 50% Ar gas mixture (Figs. 4.1, 4.3, 4.5 and 4.6). Note that the relatively large (50-75%) fractions of silicon in the C-Si-B target erosion area and relatively high concentrations of argon in the N$_2$-Ar gas mixture, were found to be optimum for the production of hard and highly elastic Si-B-C-N films with very high oxidation resistance (see Refs. 2 and 3 and chapter 3).

Evolution of the compressive stress generated in films under various experimental conditions is shown in Figs. 4.6-4.9. Fig. 4.10 provides information on a possibility to control electrical conductivity of the Si-B-C-N films with a high carbon content by means of the negative substrate bias voltage.
Chapter 4 - Influence of substrate bias voltage

4.2 Results

4.2.1 Discharge and deposition characteristics

Figures 4.1 and 4.2 show the influence of substrate bias on discharge and deposition characteristics in the case of sputtering of Si-B-C-N materials (for details on their evaluation see chapter 2, section 2.1.2). The discharge characteristics are observed for (1) the dc discharge near the sputtered target (absorbed power $P_{dc}$ and sputtering current $I_m$), and (2) the rf discharge near the substrate holder (absorbed time-average power $P_{rf}$ and substrate bias voltage $U_b$).

Figs. 4.1(a) and 4.2(a) show that at higher $|U_b|$ values, resulting in an increased $P_{rf}$ power, the $P_{dc}$ power decreases (as a consequence of the decreased $U_{dc}$ voltage applied to keep a constant value of $I_m = 1$ A) due to a mutual coupling between both discharges. The corresponding $P_{dc}$ and $P_{rf}$ values are systematically higher for a 25% N$_2$ + 75% Ar gas mixture (Fig. 4.2(a)). The main reason for this is an increased plasma impedance leading to a higher $P_{dc}$ power$^{2,4}$. The higher (75%) fraction of argon in the discharge gas, together with the related increased $P_{dc}$ value, resulted in a progressive rise in the deposition rate of the films due to more effective physical sputtering of both composite targets with a 60% silicon fraction in the

![Discharge and deposition characteristics](image-url)

**Fig. 4.1:** Discharge and deposition characteristics of films prepared using a C-Si-B (20:60:20 %) target at various negative substrate bias voltages in a 50% N$_2$ + 50% Ar gas mixture for $T_s = 350$ °C (full symbols) or $T_s = 180$-250°C (empty symbols). Panel (a) shows deposition rate and powers, $P_{dc}$ and $P_{rf}$, absorbed in the discharge. Panel (b) shows ions to film-forming particles flux ratio, $\Gamma_i/\Gamma_p$, and energy delivered by ions into growing films per one film atom.
erosion area. In the case of the B\textsubscript{4}C-Si target the measured deposition rates are even systematically higher in spite of lower P\textsubscript{dc} powers. This is mainly caused by a higher total sputtering yield and secondary electronic emission coefficient of the sputtered material. As is seen in Fig. 4.1(a), a higher substrate temperature T\textsubscript{s} = 350 °C leads to a small decrease of the deposition rate at lower |U\textsubscript{b}| values. This can be explained by a thermal desorption of loosely bonded species from the growing film surface.

If it is assumed that (1) the deposition rate is proportional to the flux of film-forming particles onto the substrate, Γ\textsubscript{p}, at relatively small changes in atomic density of the films, and (2) the P\textsubscript{rf} power is proportional to the respective total time-average ion flux, Γ\textsubscript{i}, then it is possible to explain the effect of the negative substrate bias voltage on the Γ\textsubscript{i}/Γ\textsubscript{p} flux ratio and the ion energy per deposited atom, E\textsubscript{ia}, presented in Figs. 4.1(b) and 4.2(b). It is shown that the low values of these quantities (Γ\textsubscript{i}/Γ\textsubscript{p} ≤ 0.2 and E\textsubscript{ia} ≤ 20 eV) at |U\textsubscript{b}| ≤ 100 V rapidly increase for |U\textsubscript{b}| > 100 V. This rise is very important for evolution of the film characteristics which will be discussed later (see, for example, stress relaxation in films, homogenization of the formed material and changes in its bonding structure, leading to a lower film hardness, or an increased Ar content and decreased H content in the films affecting their electrical conductivity).
The values of $\Gamma_i/\Gamma_p \leq 0.9$, applied in this work, are very low compared with Ref. 6 which reporting on the use of intense ion bombardment with the $\Gamma_i/\Gamma_p$ flux ratio up to 66 in magnetron sputtering of superhard materials (such as cubic boron nitride, tetrahedral amorphous carbon, boron carbide and cubic silicon carbide) with a high compressive stress (occasionally higher than 10 GPa). Because the ions are formed mainly in the dc magnetron discharge with a power $P_{dc}$ (because $P_{dc} \gg P_{rf}$ at low $|U_b|$ and $P_{dc} > P_{rf}$ at high $|U_b|$ - see Figs. 4.1(a) and 4.2(a)) being practically independent of the area of the unshielded substrate holder, $A_s$, the low $\Gamma_i/\Gamma_p$ values can be explained by the corresponding low ion fluxes $\Gamma_i$ due to the large value of $A_s = 620 \text{ cm}^2$.

4.2.2 Elemental composition and surface bonding structure

Figs. 4.3 and 4.4 present the effect of the negative substrate bias voltage on the elemental composition of Si-B-C-N films with low contents of argon, hydrogen and oxygen. Overall the influence of $U_b$ on the elemental composition of films is relatively weak. Notable exceptions are the film prepared in a 50% N$_2$ + 50% Ar gas mixture at $U_s = U_f = -38 \text{ V}$ and $T_s = 180$-$190 \text{ °C}$ when ion-induced and thermal desorption of loosely bonded C-N species from the surface of growing films are significantly reduced (Fig. 4.3), and the film with an enlarged 13 at.% carbon content prepared using a C-Si-B target in a 25% N$_2$ + 75% Ar gas mixture at $U_b = -100 \text{ V}$ and $T_s = 350 \text{ °C}$ (Fig. 4.4). The level of implanted Ar (see Fig. 4.4(b)) in the films does seem to depend on the substrate bias. Increasing substrate bias promotes the direct

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**Fig. 4.3:** Elemental composition of films prepared using a C-Si-B (20:60:20 %) target at various negative substrate bias voltages in a 50% N$_2$ + 50% Ar gas mixture for $T_s = 350 \text{ °C}$ (full symbols) or $T_s = 180$ - 250 °C (empty symbols).
implantation of Ar atoms (up to 7 at.% at the 75% Ar fraction in the discharge gas) into the films\(^4\).

As is shown in Fig. 4.4, the use of a B\(_4\)C-Si target with a fixed 40% B\(_4\)C + 60% Si erosion area resulted in appreciable changes in the elemental composition of the Si-B-C-N films compared to the C-Si-B target with a 20% C + 60% Si + 20% B erosion area. The corresponding increase in the boron content in the films (by 3 at.% at \(U_b = -100\) V and 6 at.% at \(U_b = -500\) V) and decrease of the carbon content (by 9 and 6 at.%, respectively) were connected with a rise in the silicon content (by 11 and 8 at.%, respectively) and decrease of the nitrogen content (by 6 and 8 at.%, respectively) at a slightly increased oxygen content and almost the same contents of hydrogen (around 2 at.%) and argon (up to 7 at.%).

![Fig. 4.4: Elemental composition of films prepared using a C-Si-B (20:60:20 %) target (full symbols) or B\(_4\)C-Si (40:60 %) target (empty symbols) at various negative substrate bias voltages in a 25% N\(_2\) + 75% Ar gas mixture for \(T_s = 350\) °C.](image)

The infrared spectra of Fig. 4.5 show that the negative substrate bias voltage does not cause, except possibly for the boron bonding states, significant changes in the infrared absorption of the films (for peak identifications see chapter 3). Silicon is preferentially bonded to nitrogen and to carbon except for Si-O bonds formed at the surface due to oxidation in air. It has been found that the Si-C bonds were not reliably detectable by XPS in magnetron-sputtered hard amorphous Si-C-N films\(^4,5\). Their presence in the Si-B-C-N films could be explained by a partial occupation of nitrogen bonding states by boron, which forces
Si and C to a mutual bonding. The N-Si bond is the dominant N-containing bond with a lower occurrence of N-B and N-C bonds, while the C-C bond and C-N bond are the dominant bonds for carbon atoms, with minor proportions of C-B and C-Si.

Boron is preferentially bonded to nitrogen with a lower occurrence of the B-C bonds. Relatively highest abundance of the B(sp\(^3\))-N bonds can be observed in Fig. 4.5 for the films prepared at \(U_b = -100\) V and \(T_s = 350\) °C. This phenomenon, confirmed also by XPS measurements, is in agreement with Ref. 11, reporting on existence of a window of ion energies for which B(sp\(^3\))-N bonds dominate in sputtered amorphous BN films.

![Fig. 4.5: The dependence of the absorption coefficient on wavelength in the infrared region, obtained by IR VASE for films prepared using a C-Si-B (20:60:20 %) target at various negative substrate bias voltages in a 50% N\(_2\) + 50% Ar gas mixture for \(T_s = 350\) °C (solid lines) or \(T_s = 180-250\) °C (dashed lines).](image)

4.2.3 Mechanical properties

Figs. 4.6 and 4.7 present the effect of the negative substrate bias voltage on the mechanical properties of Si-B-C-N films. A negative substrate bias voltage of \(U_b = -100\) V with the corresponding low values of \(\Gamma_i/\Gamma_p \leq 0.2\) and \(E_{ia} \leq 20\) eV (see Figs. 4.1(b) and 4.2(b)) was found to be almost optimum for formation of hard densified amorphous Si-B-C-N materials (density around 2.4 g/cm\(^3\)) with strong local covalent bonds. Fig. 4.6 shows that the values of all examined mechanical quantities (hardness, modified Young's modulus \(E/(1-\nu^2)\) and elastic recovery) are substantially higher (44 GPa, 240 GPa and 82%, respectively) at \(U_b = -100\) V for the increased substrate temperature \(T_s = 350\) °C, probably due to a higher fraction of B(sp\(^3\))-N and C(sp\(^3\))-N bonds in the films\(^{10}\). Note that the level of intrinsic compressive stress is not strongly varying, hence the variations in the other properties are not the result of variations in the stress level. As is seen in Fig. 4.6(a), there is practically no
correlation between film hardness and low values (close to 1 GPa) of compressive stress in the films prepared in a 50% N\textsubscript{2} + 50% Ar gas mixture. However, an intensified bombardment of growing films by argon ions in a 25% N\textsubscript{2} + 75% Ar gas mixture resulted in U\textsubscript{b} dependent values of the compressive stress with a maximum value of 1.8 GPa achieved at U\textsubscript{b} = -125 V for the films prepared using the C-Si-B target (Fig. 4.7(a)). The values obtained for all the aforementioned mechanical quantities were systematically higher than those obtained with the corresponding B\textsubscript{4}C-Si target.

Besides promoting the formation of the B(sp\textsuperscript{3})-N and C(sp\textsuperscript{3})-N bonds, another possible explanation of the observed effect of U\textsubscript{b} in increasing film hardness, has been suggested by results of molecular-dynamics simulations\textsuperscript{13}. Because the results are described in detail in chapters 7 and 8, here we only note that using a liquid-quench algorithm, which allows to simulate rapid (low |U\textsubscript{b}|) and slow (high |U\textsubscript{b}|) cooling of the localized melt formed around sites of energetic ion impact, two types of segregation leading to a higher extrinsic hardness of the Si-B-C-N films prepared at U\textsubscript{b} = -100 V were predicted.

Hardness enhancements due to segregation of phases have been reported previously for binary mixtures of various amorphous and nanocrystalline phases\textsuperscript{14}. The MD simulations

![Graph](image-url)

**Fig. 4.6:** Hardness measured with the presented maximum load and intrinsic compressive stress (a), and effective Young’s modulus, E/(1 - \nu\textsuperscript{2}), and elastic recovery measured with a maximum load of 30 mN (b) for films prepared using a C-Si-B (20:60:20 \%) target at various negative substrate bias voltages in a 50% N\textsubscript{2} + 50% Ar gas mixture for T\textsubscript{s} = 350 \degree C (full symbols) or T\textsubscript{s} = 180 - 250 \degree C (empty symbols).
showed that small segregated regions, which occur as a result of random clustering in a melt were able to survive rapid cooling stage and become locked into the structure. The thermodynamically preferred structure, which has been found to be homogeneous, forms with slow cooling (high $|U_b|$). Another type of phase segregation observed is the formation of silicon-enriched zones around implanted argon atoms. While at high Ar content (around 6 at.%) for $U_b = -500$ V most of the network atoms are close to at least one Ar atom, which in fact leads to an almost homogeneous Si-B-C-N material, the occurrence of both Si-rich (close-to-Ar) and Si-poor (far-from-Ar) zones can be observed at a lower (1-2 at. %, see Figs. 4.3(b) and 4.4(b)) Ar content for $U_b = -100$ V. The energy advantage gained by surrounding Ar atoms with longer and more flexible Si-containing bonds was proposed to be a driving force for this segregation. This will be discussed in more detail in Chapters 7 (segregation around Ar) and 8.2 (its possible effect on hardness).

4.2.4 Compressive stress in the films

For films deposited above room temperature a component of the stress measured at room temperature is so called extrinsic stress, due to differences in thermal expansion coefficients of the film and the substrate. For our Si-B-C-N films we estimate this component to be

\[ \left( \frac{E}{1 - \nu^2} \right) \text{ (GPa)} \]

where $E$ is the Young's modulus and $\nu$ is the Poisson's ratio.

Fig. 4.7: Hardness measured with the presented maximum load and intrinsic compressive stress (a), and effective Young’s modulus, $E/(1 - \nu^2)$, and elastic recovery measured with a maximum load of 30 mN (b) for films prepared using a C-Si-B (20:60:20 %) target (full symbols) or $B_4C$-Si (40:60 %) target (empty symbols) at various negative substrate bias voltages in a 25% $N_2 + 75%$ Ar gas mixture for $T_s = 350$ °C.
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\[ \sigma_{\text{CTE}} = |E(\alpha_f - \alpha_s)(T_s - T_r)| < 0.1 \text{ GPa} \]  
\hspace{1cm} (Eq. 4.1).

using typical values of the coefficients of thermal expansion (CTE) in the relevant temperature range, \( \alpha_f \approx 1.8 \times 10^{-6} \text{ K}^{-1} \) (see Ref. 15) for the Si-B-C-N and \( \alpha_s \approx 2.8 \times 10^{-6} \text{ K}^{-1} \) for the silicon substrate and assuming that the films Young’s modulus \( E < 300 \text{ GPa} \). This suggests that a major part of the measured film stress is caused by deposition conditions, particularly by ion bombardment of growing films.

The dependence of the compressive stress on the substrate bias voltage, \( U_b \), was most pronounced for the films prepared using the C-Si-B target in a 25% \( N_2 + 75\% \text{ Ar} \) gas mixture (see Fig. 4.7(a)). We used a simple theoretical model developed by Davis\(^{16}\) to compare with the results in Fig 4.8. The model captures the formation of the compressive stress \( \sigma(E_i) \) by ion bombardment, considering a steady state in which the stress formation by knock-on implantation of film atoms due to bombarding ions is balanced by the ion-energy induced migration of the implanted atoms. The Davis model is given by the equation\(^{16}\)

\[ \sigma(E_i) = \frac{E}{1 - \nu} \frac{c \sqrt{E_i}}{\Gamma_p/\Gamma_i + 0.016 p(E_i/E_0)^{5/3}} \]  
\hspace{1cm} (Eq. 4.2),

where \( E \) and \( \nu \) are the Young’s modulus and the Poisson's ratio of the material, respectively, \( c \) is a constant, \( E_0 \) is the activation energy for the relaxation process and \( p \) is a material parameter of the order of 1. We recall that this model was successfully used\(^6\) for the mentioned superhard materials with a high compressive stress, produced by magnetron sputtering in a pure argon discharge, where the \( \text{Ar}^+ \) ion fluxes responsible for the stress formation in the films were relatively high in comparison with the deposition fluxes of film-forming particles (\( \Gamma_i/\Gamma_p \) up to 66).

In our calculations of \( \sigma(E_i) \), presented in Fig. 4.8, the \( E/(1-\nu) \) ratio has been replaced by the corresponding measured values of \( E/(1-\nu^2) \), see Fig. 4.7(b), under a realistic assumption that \( 1+\nu \) is approximately constant. The known values of \( \Gamma_i/\Gamma_p \), see Fig. 4.2(b),
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were used at the activation energy range from 3.5 to 5 eV and $p = 1$. As is seen in Fig. 4.8, the model of Davis describes the stress formation in the films only qualitatively in our case, when the $\Gamma_i/\Gamma_p$ flux ratio is relatively low ($\leq 0.9$) and the ions of film-forming particles (such as $N_2^+$, $N^+$ and $Si^+$) form a significant part of the total ion flux onto the substrate, $\Gamma_i$, see Ref. 2. The phenomenon that the Davis model (which is empirical and therefore doesn’t incorporate the physics of stress relief by ion energy) tends not to fit the falloff of stress seen as the ion energy is increased after the peak is discussed more closely in recent Ref. 12.

In addition to the low $\Gamma_i/\Gamma_p$ values, a high Si content in materials produced using the C-Si-B and B$_4$C-Si targets with a 60% Si fraction in the erosion area (Figs. 4.3(a) and 4.4(a)) is another reason for low values ($\leq 1.8$ GPa) of their compressive stress (Figs. 4.6(a) and 4.7(a)). This beneficial role of silicon in reducing the compressive stress has been already suggested at the end of chapter 3, and in Fig. 4.9 it is shown together with respective values of hardness for the Si-B-C-N films prepared in a 25% $N_2 + 75\%$ Ar gas mixture at $U_b = -100$ V and $T_s = 350 \, ^{\circ}C$ using a B$_4$C-Si target with the Si fraction in the erosion area varied from 5 to 75%. As can be seen in Fig. 4.9(a), the increasing Si fraction in the target erosion area led to a rising incorporation of silicon (from 8 to 46 at.%) into the films. As a result, the film hardness rapidly increased to a saturated value of 32 GPa, while the corresponding compressive stress in the films successively decreased from 1.7 to 0.9 GPa (Fig. 4.9(b)).

The ability of silicon to reduce that part of the compressive stress which is generated by implanted Ar atoms has been explained in Ref. 13 - see chapter 7 for detailed discussion. Using liquid-quench molecular dynamics simulations, the aforementioned segregation of Si

![Graph](image)

**Fig. 4.9:** Hardness and compressive stress correlated with the Si content in films prepared in a 25% $N_2 + 75\%$ Ar gas mixture at various Si fractions in the erosion area of the B$_4$C-Si target for $U_b = -100$ V and $T_s = 350 \, ^{\circ}C$. 

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atoms around Ar-containing "cavities" during solidification of the material and increased preference of other atoms to bond with Si in vicinity of these cavities have been shown. The comparative flexibility of the long Si-containing bonds enables these bonds to deform to accommodate the argon atoms into the structure with a minimum generation of stress.

4.2.5 Electrical conductivity

Fig. 4.10 presents the results obtained for electrical resistivity of films prepared in two different N\textsubscript{2}-Ar gas mixtures using a modified C-Si-B target with a high C fraction (75\%) and low Si fraction (5\%) in its erosion area. This modification allowed us to form semiconductive Si-B-C-N materials. Neglecting low contents of Ar, H and O in the films, their typical elemental composition can be characterized as Si\textsubscript{10}B\textsubscript{12}C\textsubscript{40}N\textsubscript{38}. As can be seen in Fig. 4.10, the electrical resistivity of the films prepared in a 50\% N\textsubscript{2} + 50\% Ar gas mixture rapidly decreases (almost 100 times in the range from \(U_b = U_f\) to \(U_b = -700\) V) with a rise in the \(|U_b|\) values. This can be explained (1) by a decreasing occurrence of weakly bonded hydrogen atoms (inhibiting interconnections between other film atoms and thus decreasing the electrical conductivity of films\textsuperscript{17}) in the film volume due to the ion bombardment, or (2) by turning of sp\textsuperscript{3}-rich structure into a sp\textsuperscript{2}-rich one (which is generally known to be more conductive). In this particular case, the first explanation is more probable because (1) the increase in conductivity starts immediately above floating voltage (i.e. not above some \(U_b\) threshold), and (2) at high carbon content the hardness (which is there likely to correlate with the sp\textsuperscript{3}/sp\textsuperscript{2} ratio) is higher at higher \(|U_b|\) of 500 V (see chapter 3, section 3.3.1).

However, a different trend was observed for the films prepared in a 25\% N\textsubscript{2} + 75\% Ar gas mixture, for which electrical resistivity increased at \(|U_b| > 300\) V. We believe that this behaviour is caused by a stronger Ar\textsuperscript{+} ion bombardment leading to a higher content of implanted argon atoms in the films. As a result, a dense 3D structure of Si-B-C-N materials is replaced by a structure consisting of 2D-like zones around large (radius >2 Å) cavities including implanted Ar atoms\textsuperscript{13}. This structural change of the Si-B-C-N network leads to a decrease in the electrical conductivity of films prepared at high \(|U_b|\) values in N\textsubscript{2}-Ar gas.

Fig. 4.10: Electrical resistivity of films prepared using a C-Si-B (75:5:20 \%) target at various negative substrate bias voltages in a 50\% N\textsubscript{2} + 50\% Ar (full symbols) or 25\% N\textsubscript{2} + 75\% Ar (empty symbols) gas mixture for \(T_s = 350\) °C.
mixtures with high Ar fractions, when an already low volume concentration of hydrogen in
the films cannot be further reduced while the content of implanted argon steadily increases.

### 4.3 Conclusions

Novel quaternary Si-B-C-N films were fabricated using dc magnetron co-sputtering of
silicon, boron and carbon from a single C-Si-B (20:60:20 % and 75:5:20 %) or B₄C-Si (40:60 %)
target in nitrogen-argon (50:50 % and 25:75 %) gas mixtures at various rf induced
negative substrate bias voltages (from floating potential to \( U_b = -700 \) V) and substrate
temperatures \( T_s \) in the range 180-350 °C. The films, typically 2-5 μm thick, were found to be
amorphous with a density around 2.4 g/cm³ and good adhesion to substrates with a low
compressive stress (0.6-1.8 GPa). It was shown that the negative substrate bias voltage
\( U_b = -100 \) V with the corresponding low values of the ion-to-film-forming particles flux-ratio
\( \Gamma_i/\Gamma_p \leq 0.2 \) and the ion energy per deposited atom \( E_{ia} \leq 20 \) eV are about optimum at
\( T_s = 350 \) °C for the formation of hard (hardness up to 44 GPa) and highly elastic (elastic
recovery up to 82 %) Si-B-C-N films with a high (27-40 at.%) silicon content, exhibiting
extremely high oxidation resistance in air at elevated temperatures (up to the 1350 °C
substrate limit), see our recent works 2,3. A beneficial role of silicon in reducing the
compressive stress in the films was observed. The electrical conductivity of the
semiconductive Si-B-C-N films with a high (approximately 40 at.%) carbon content was
controlled over a wide range (almost two orders of magnitude) by the nitrogen-argon gas
mixture composition and the \( U_b \) values.

### 4.4 References

2. J. Vlček, Š. Potocký, J. Čížek, J. Houška, M. Kormunda, P. Zeman, V. Peřina, J. Zemek,
5 Formation of N\textsubscript{2} molecules in rapidly quenched amorphous materials

This chapter is based on results published in Ref. 1. It includes ab-initio molecular dynamics simulations of the preparation of CN\textsubscript{x}, B-C-N and Si-B-C-N materials formed by energetic ion assisted deposition techniques. We focus on the formation of N\textsubscript{2} molecules during liquid quench simulations and investigate how density, temperature and quench rate affect the number of N\textsubscript{2} molecules formed in the network. We find that higher material density and shorter cooling times lead to reduced N\textsubscript{2} formation and thus higher nitrogen incorporation into the structure. These results suggest a modification of common physical vapour deposition (PVD) techniques to enhance N content in materials such as CN\textsubscript{x}.

5.1 Introduction

The crystalline β-C\textsubscript{3}N\textsubscript{4} phase, in which the carbon is tetrahedrally coordinated, promises high hardness. Thus, we would expect that amorphous CN\textsubscript{x} materials with high N content (~57\%) should incorporate tetrahedrally coordinated carbon and show similar properties. However, there appear to be clear limits to how much nitrogen can be incorporated in CN\textsubscript{x} or other amorphous N-containing materials such as Si-B-C-N. In particular, CN\textsubscript{x} samples prepared to date are limited in N content to below approximately 35\% with mostly sp\textsuperscript{2}-bonded carbon. For materials prepared by plasma sputtering, these limits may be due to a thermodynamic preference to pair N atoms into free N\textsubscript{2} molecules instead of incorporating them into the amorphous network.

In this chapter we report ab initio molecular dynamics liquid quench simulations of N-rich amorphous CN\textsubscript{x} and Si-B-C-N materials, in which we observe the formation of N\textsubscript{2} molecules under typical deposition conditions. We closely examine the formation of N\textsubscript{2} molecules in liquid quench simulations and propose a novel algorithm that suitably removes N\textsubscript{2} molecules in the course of a simulation. Using this algorithm, we identify the main factors that minimize the amount of N\textsubscript{2} formed and therefore maximize the N-content in deposited materials. This suggests experimental conditions that could potentially lead to novel materials with enhanced N content.

Simulations here focus on one Si-B-C-N material with composition Si\textsubscript{14}B\textsubscript{23}C\textsubscript{6}N\textsubscript{57} and one B-C-N material with composition B\textsubscript{41}C\textsubscript{8}N\textsubscript{51}. Other elements detected in these samples in small quantities (Ar < 3 at.\%, H < 4 at.\%) were neglected. The Si-B-C-N sample was chosen because of its relatively high nitrogen content, which facilitates the study of N\textsubscript{2} formation processes during liquid-quench simulations. The B-C-N sample was chosen because it was prepared under similar conditions to the Si-B-C-N sample except for the absence of Si in the sputter target.

5.2 Results

5.2.1 N\textsubscript{2}-formation during liquid quench simulation

Liquid quench simulations were performed for the Si-B-C-N and B-C-N compositions described above. These were carried out using a simulation cell containing 100 atoms with the cell volume set to match the experimental atomic density. The exponential cooling time from 5000 to 650 K was 100 fs; this is shorter than the 500 fs used for SiC simulations in Ref. 2 in
accordance with the higher thermal diffusivities for various amorphous Si-C-N and B-C-N materials reported in Ref. 3.

![Diagram](image)

**Fig. 5.1:** Snapshots from the liquid-quench simulation of a Si-B-C-N material of composition Si$_{14}$B$_{23}$C$_6$N$_{57}$ (panel a) and a B-C-N material of composition B$_{41}$C$_8$N$_{51}$ (panel b). Five N$_2$ molecules formed during the liquid-quench phase of the simulation in the Si-B-C-N sample and four in the B-C-N sample are present. Large black circles are C, dark grey are N, light grey are B, white circles correspond to Si, the small black dots represent Wannier function centres (WFCs).

Typical Si-B-C-N and B-C-N structures that are obtained at the end of the exponential cooling and subsequent equilibration run are shown in Figs. 5.1(a) and (b). Clearly seen in Fig. 5.1(a) are five N$_2$ molecules that are not covalently bonded to the amorphous network. Inspection of the molecular dynamics trajectories reveals that these molecules were formed during the cooling and equilibration and remained trapped in the cell. Similarly, at the end of
the simulation for the B-C-N material four N$_2$ molecules were found. N$_2$ formation during liquid quenching was also reported for BN material in Ref. 4, but without any detailed analysis.

We expect that every N$_2$ molecule formed during the synthesis escapes from the deposited material since the thermal spike in which the molecules are formed is always close to the material surface. Repeated thermal spikes at the same location would also facilitate N$_2$ out-diffusion. The absence of N$_2$ molecules was experimentally confirmed by thermogravimetric analysis$^3$, which revealed no mass loss (indicative of N$_2$ outgassing) up to 1300 °C.

In order to explore the effect of atomic density on the number of N$_2$ molecules formed, identical liquid-quench simulations for these two materials were carried out with atomic densities increased by 10, 20 and 30 % relative to the experimental density. Figure 5.2 shows that an increase in the simulation density leads to a reduction in the number of N$_2$ molecules formed. This indicates that high-density networks have the potential to incorporate more nitrogen. The calculated stresses for both the Si-B-C-N and B-C-N compositions are compressive and substantially larger for B-C-N. While our simulation method consistently overestimates stress values and does not account for any long time scale post-deposition stress relief processes, some observations can be made regarding relative stresses. Our findings are in qualitative agreement with the experimentally measured stresses of -1.15 and -2.34 GPa for the Si-B-C-N and B-C-N samples, respectively. For both the samples, the compressive stress increases significantly with increasing density beyond a second point of the dependence, while the reduction in slope of the compressive stress between the first and second points to the decrease in the molecular N$_2$ content.

![Fig. 5.2: The effect of simulation density on calculated compressive stress and on the number of N$_2$ molecules formed. Numbers in parentheses indicate the numbers of N$_2$ molecules formed during the simulation.](image-url)
Chapter 5 - Formation of N₂ molecules

**Figure 5.3:** The predicted effect of the density of deposited Si-B-C-N materials on the occurrence of single, double and triple bonds of all kinds in the network. Triple bonds associated with N₂ molecules are not included.

Figure 5.3 shows the average percentages of single, double and triple bonds as a function of the density of the simulated sample. The data shows that an increase in density leads to an increase in the ratio of single to double bonds. Increased density results in increased coordination numbers and hence a tendency towards reduced bond order. In the case of nitrogen, this is reflected in a reduction in triple bonds present in N₂ molecules in preference for single and double bonds linking nitrogen into the network.

**Figure 5.4:** A snapshot from the liquid-quench simulation of a Si-B-C-N material of composition Si₁₄B₂₃C₆N₅₇. Thirty-two extra nitrogen atoms were added at the start of the simulation and seventeen N₂ molecules were removed during the liquid quench. The final elemental composition is therefore Si₁₄B₂₃C₆N₅₅. The large black circles are C, dark grey are N, light grey are B, white correspond to Si and the small black dots represent Wannier function centres.
5.2.2 Liquid quench simulations with N$_2$ removal

The fact that our initial simulations lead to the formation of N$_2$ molecules in the network that are not confirmed in experiment, prompted us to revise our simulation strategy. Exponential cooling and equilibration MD runs were stopped at regular intervals in order to remove any N$_2$ molecules from the simulation cell. After each N$_2$-removal, the simulation volume was adjusted so that the atomic density was maintained. A wave function optimisation was performed before the MD simulation was resumed. This modified liquid quench algorithm leads to final structures that do not contain any N$_2$ molecules and are therefore likely to be better representations of the experimental materials. In order to obtain a final structure with desired N-content, these simulations need to be started with nitrogen atoms in excess of the experimental N-content in the expectation that N$_2$ molecules will be formed and removed during the simulation. As mentioned previously, it is likely that N$_2$ molecules form and diffuse out of the structure during synthesis. Three such simulations on Si-B-C-N were performed containing 0, 16 and 32 extra nitrogen atoms in addition to the 100 atoms of experimental elemental composition (Si$_{14}$B$_{23}$C$_6$N$_{57}$). After approximately 1 ps of equilibration, this new algorithm leads to stable structures and N$_2$ molecule formation stops. The final structures (e.g. Fig. 5.4) do not contain any N-N triple bonds (e.g. azide – N$_3$) that could potentially lead to N$_2$ molecules after longer simulation times.

Fig. 5.5 shows that simulations with a sufficiently high number of extra nitrogen atoms at the start of the simulation lead to final structures with the desired experimental composition. With an exponential cooling time of 100 ps, a nitrogen-excess of 0, 16 and 32 N atoms resulted in final nitrogen contents of 51, 55 and 56 at.%, to be compared with 57 at.% in the experimental sample. However, The method requires some tuning to achieve a particular N concentration in the simulated structure because not only the starting nitrogen content but also the cooling time influences on the number of N$_2$ molecules formed and thus the final nitrogen content.

Fig. 5.5: The total nitrogen content as a function of simulation time during liquid-quench simulations of the Si-B-C-N material (Si$_{14}$B$_{23}$C$_6$N$_{57}$) with removal of N$_2$ molecules after formation. Three simulations, which started with a nitrogen excess of 0, 16 and 32 atoms beyond the 100 atoms of experimental composition, resulted in structures with different final N-content. The shaded area marks the experimental N-content (with ±2 % error). The exponential cooling time was 100 fs.
Chapter 5 - Formation of N\textsubscript{2} molecules

The fact that the final N-content depends strongly on the cooling time is illustrated in Figure 5.6. This figure shows our results for a CN\textsubscript{x} material (composition C\textsubscript{44}N\textsubscript{88}, mass-density 3g/cm\textsuperscript{3}) for which liquid-quench simulations with different exponential cooling times (100, 200 and 500 fs) lead to different nitrogen contents. Longer exponential cooling times lead to the formation of more N\textsubscript{2} molecules during cooling and hence lower N-content in the final structure, 63, 61 and 58 at.% for cooling times of 100, 200 and 500 fs, respectively. This indicates a possibility of enhancing the nitrogen content in materials such as CN\textsubscript{x} prepared by physical vapour deposition (PVD) methods by increasing the cooling rate. This could be achieved, for example, by decreasing the substrate surface temperature during the deposition.

5.2.3 The temperature window for N\textsubscript{2} formation.

The formation of N2 molecules requires sufficient energy to break bonds containing N atoms that are part of the network and to enable the diffusing N atoms to find one another before forming another bond. We have observed in our simulations that at temperatures below 650 K no further N\textsubscript{2} formation takes place. The thermal energy is there insufficient for the extraction of N atoms out of the network. At sufficiently high temperatures N atoms remain non-bonded because the thermal energy is too high for any N\textsubscript{2} molecules to remain undissociated. In earlier work\textsuperscript{6,7}, it was found that significant thermal N\textsubscript{2} dissociation required temperatures of 8000 K or more. Together, these two observations suggest that there exists a temperature window for the formation of N\textsubscript{2} molecules in PVD processes. Here we are particularly interested in the lower boundary of this temperature window.

In order to determine the temperature window within which N\textsubscript{2} formation is likely, we performed a series of constant temperature MD simulations with temperatures between 1000 and 7000 K. These simulations were started using a single molten structure of composition C\textsubscript{44}N\textsubscript{86}, which was generated using the initial mixing run (see the description of the liquid-quench algorithm in section 2.2.2) N\textsubscript{2} molecules which formed during the mixing were removed from the structure. The structure was then wavefunction optimized and initial velocities appropriate for the constant temperature simulation were allocated. As in the previous liquid quench simulations, N\textsubscript{2} molecules were removed from the simulation cell at
regular intervals. With this type of simulation we were able to examine the rate of N$_2$ formation as a function of temperature and thereby characterise the temperature window.

Figure 5.7 shows the number of N$_2$ molecules formed (and removed) after 200, 400 and 800 fs simulation times as a function of temperature. The figure clearly shows that the maximum rate of N$_2$ formation occurs between 4000 and 5000 K, with a maximum of 19 N$_2$ molecules formed after 800 fs at 5000 K. Note that a number of N atoms start out in close proximity and are prone to form N$_2$ molecules immediately. This phenomenon led to eight N$_2$ molecules forming at 1000 K where diffusion does not play a significant role. These N$_2$ molecules are not of relevance to the temperature window, since they do not involve diffusion processes or the release of N atoms from the network. Above 1000 K, the rate of N$_2$ formation steadily increases until a maximum at 5000 K is reached. Above 5000 K, the rate progressively decreases because two N atoms encountering each other are increasingly likely to carry too much thermal energy to form a stable N$_2$ molecule. Our constant temperature simulations show that the temperature window with effective N$_2$ formation occurs between 3000 and 6000 K.

![Figure 5.7: The number of N$_2$ molecules formed in the C$_{44}$N$_{86}$ sample during 800 fs long MD runs at various temperatures. In the lower temperature part of the figure, the first eight N$_2$ molecules arise from 16 N atoms that start out in close proximity to one another. At 1000 K, these eight N$_2$ molecules are the only ones formed. Between 1000 and 5000 K additional N$_2$ molecules form through diffusion. Above 5000 K, the formation of N$_2$ molecules is prevented by the high thermal energy of diffusing N atoms.](image)

5.2.4 Discussion

The simulations presented in this chapter are relevant to the PVD preparation of nitrogen containing materials such as CN$_x$, B-C-N and Si-B-C-N. In PVD processes, ion bombardment leads to local melting (thermal spike) at the site of impact. The rate of cooling and solidification depends on the thermal diffusivity of the target material. Our results, showing a temperature window, suggest that loss of nitrogen from the network occurs above approximately 3000 K through the formation of N$_2$-molecules. This suggests further that nitrogen uptake into deposited CN$_x$ amorphous networks can be improved by reducing the time spent in this active temperature window. This could be accomplished by:
Improved deposition processes, that incorporate these principles, may lead to materials with enhanced N-content. In order to quantify the effect of different target (substrate) temperatures on the time spent in the active temperature window, we used the expression for cooling of a hemispherical thermal spike of radius $r_0$ as developed in Ref. 8 for tetrahedral amorphous carbon. This expression assumes a constant thermal diffusivity of the material and allows us to estimate the temperature as a function of time for thermal spikes formed in materials held at various target temperatures. Hence, we can estimate the time, which the material spends in the active temperature window for N$_2$ formation (3000-6000 K). Figure 5.8 shows the result for a point halfway between the centre and the boundary of a hemispherical thermal spike.
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5.3 Conclusions

In MD liquid quench simulations of Si-B-C-N, B-C-N and CN\textsubscript{x} amorphous materials we have observed the formation of free N\textsubscript{2} molecules. We have identified a temperature window in which stable N\textsubscript{2} molecules are formed. Our results show that the final N-content in networks of given Si/B/C ratios depends both on the time spent in the active temperature window and on the density of the material. Higher coordination numbers occur in more dense materials and allow incorporation of more N into the network. An increase in the cooling rate is identified as a means of decreasing the time spent in the temperature window for N\textsubscript{2} formation and thus increasing the N-content of a given network. Cooling the sample during preparation is found to have limited potential for increasing the cooling rate; however, using lower energies of impact during growth may achieve higher N-content by forming smaller and hence more rapidly quenched thermal spikes. High N-contents are also expected for Si/B/C compositions with high thermal diffusivity.

5.4 References

6 A new method for obtaining desired compositions in liquid-quench simulations of nitrogen-containing materials

This chapter is based on results included in Ref. 1. A modified liquid-quench algorithm with a flexible cooling time which can lead to desired compositions of N-containing materials without any N₂ molecules in their final structure is described here. It solves the problem presented in the previous chapter 5 (formation of N₂ molecules in the simulation cell during classical liquid-quench simulations). The new algorithm presented here was used to obtain the simulation results presented in the following chapters 7 and 8.

6.1 Introduction

As we have shown in the previous chapter 5, molecular dynamics (MD) simulation of N-containing materials such as CNₓ or Si-B-C-N may lead to the formation of N₂ molecules in the simulation cell. These molecules are likely to diffuse out of the real material during deposition, whereas they are normally prevented from doing so in the simulation and remain trapped in the cell. We have shown that a certain nitrogen excess in the starting cell can when used with an appropriate cooling rate lead to a structure with approximately the desired N content if all of the N₂ molecules are removed after forming. However, the determination of an appropriate cooling time can be very computationally expensive. Moreover, it is desirable not to fix the cooling time because variations in cooling time are often used in the liquid-quench protocol for simulating ion bombardment at different energies. The energy of the ion impact determines the size of the molten region and hence its cooling rate.

In this chapter, we present a modified liquid-quench algorithm with a flexible cooling time which can lead to predetermined compositions of N-containing materials without N₂ molecules in their final structure. We justify the algorithm by studying the bond-forming and bond-breaking processes in CNₓ, BNₓ and SiNₓ materials at various temperatures and comparing with experimental data where possible.

We studied the bond-forming and bond-breaking processes in the sample C₄₄N₈₆ of density 3g/cm³ by performing 0.5 ps long constant-temperature MD runs at various temperatures up to 7000 K. To determine equilibrium properties of the structure, 0.5 ps long constant-temperature MD runs were performed for samples B₄₄N₈₆ and Si₄₄N₈₆ of the same atomic density at 5000 K only. Prior to the constant-temperature MD runs, each sample has been mixed by melting in order to remove memory of the initial configuration.

6.2 Specific methodology

Because we did not calculate positions of Wannier function centres (WFCs) during these simulations, the bonding analysis in this chapter is based on the use of bonding distance cutoffs. Two network atoms were considered to be bonded if their distance was ≤2.0 Å for C-C, ≤1.9 Å for C-N, ≤2.1 Å for B-B, ≤2.1 Å for B-N, ≤2.8 Å for Si-Si, ≤2.2 Å for Si-N and ≤1.8 Å for N-N pairs. A N₂ molecule was considered to be formed if in two consecutive snapshots of the structure the distance of two N atoms was ≤1.3 Å and these atoms were bonded only to each other. The triple bond between these two N atoms was then considered to be broken or converted to single or double bond when distance between these atoms increased to ≥1.6 Å. Temporary bonding of the N₂ molecule to the network wasn't considered as a breaking of the molecule. This choice of these maximal bond lengths leads to maximal calculated lifetimes of network bonds, and a ratio of around 1.25 for the maximal to average
(as identified by WFCs) bond lengths (single for network bonds, triple for N₂ molecules) for all bonds.

6.3 Results

6.3.1 The modified liquid-quench algorithm

When a MD simulation of N-containing material is commenced, a number of N₂ molecules form immediately due to the random presence of some N pairs in close proximity in the starting configuration (see the previous chapter 5). This is followed by formation of additional molecules as a result of diffusion and bond-breaking processes. An example of a simulated CNₓ sample including free N₂ molecules is shown in Fig. 6.1, with Wannier function centres representing pairs of valence electrons.

In order to compensate for N atom loss and still achieve a desired N-content in the quenched material, the liquid quench simulation was commenced with a substantial N-excess. In the previous chapter, we identified a temperature window for N₂ formation in alloys of this type between 3000 and 6000 K. Below 3000 K, N-N pairs which previously formed a triple bond can leave the network and form a free molecule, but no new triple N-N bonds form. In the light of this information we modified some stages of the liquid quench algorithm. The new algorithm is described below with examples taken from Ref. 9 for simulations of previously deposited amorphous materials. At the end of each stage, any new N₂ molecules formed are removed, the cell dimension is scaled in order to keep the atomic density constant and the wavefunction is optimized.

**Figure 6.1.** Snapshot from the liquid-quench simulation of a CNₓ material of composition C₄₄N₈₆. Six of the triple-bonded N-N pairs (free N₂ molecules or their precursors) formed during the simulation are denoted by arrows. Large dark circles are C, large light circles are N and the small black dots represent Wannier function centers.
(1) **Starting Structure**: An initial structure is generated by distributing 100 atoms of the experimental composition with up to 32 additional N atoms distributed semi-randomly over the simulation cell of a dimension chosen to give the desired atomic density. The optimal N-excess for various samples increases with decreasing atomic density, that is, with increasing rate of N₂ formation.

(2) **Initial Mixing**: In order to obtain a completely randomized structure with no memory of the initial structure, a 1 ps MD run at a temperature above melting point (5000 K - Nose-Hoover [NH] thermostat) is carried out. A plane-wave cut-off of 10 Ry is sufficient for this stage of the simulation where high accuracy of the DFT energies is not required. The low cut-off increases the efficiency of the simulation, and was also found useful as it effectively prevents the formation of stable bonds which would interfere with efficient mixing.

(3) **N₂ Removal Run**: The previously used exponential cooling applied to temperatures above 3000 K (that is, inside the temperature window for N₂ formation) is now replaced by a constant temperature MD run of flexible length. The target temperature chosen for this run is above the temperature at which stable network bonds start to form, so we can use its length to control the amount of N₂ formation without affecting the final structure. During this run, the structure is inspected at regular intervals (every 50 fs) using Wannier function analysis. The run is stopped when the number of N atoms involved in either free N₂ molecules or in other triple bonded N-N pairs is equal to the starting N excess. This criterion is based on our experience which has shown that triple-bonded pairs of network N atoms are early precursors of N₂ molecules.

(4) **Exponential Cooling**: The resulting material (having the desired composition with additional triple-bonded N-N pairs) is exponentially cooled down from (only) 3000 K to the target (i.e. substrate) temperature. Temperature control is achieved by rescaling the velocity of ions when the actual and target temperatures differ by more than 10%. By adjusting the cooling time in this phase of the simulation, it is still possible to simulate the effect of varying ion bombardment energies. In our simulations, most of the remaining N-N triple bonds were converted to N₂ molecules during the exponential cooling.

(5) **Equilibration**: The rest of the liquid-quench algorithm is unchanged. After the cooling phase, sample equilibration is accomplished using a 1 ps MD run at deposition temperature (NH thermostat). The purpose of equilibration is for the system to fully recover thermal equilibrium as indicated by a constant mean squared displacement.

(6) **Production Run**: Following equilibration, various quantities of interest (such as bonding statistics or stress) can be computed as statistical averages over a MD run of a minimal length of 0.5 ps at deposition temperature.

### 6.3.2 Temperature of the N₂ removal run

The N₂ removal run has to be accomplished at sufficiently high temperature, above the melting point at which no stable network bonds form so that the high mobility of atoms allows diffusion and bond-breaking processes, leading to formation of N₂ molecules. However, the temperature must be also sufficiently low to ensure stability of the N₂ molecules formed. This prompted us to find a temperature window fulfilling these conditions by studying bond-forming and bond-breaking processes in a sample of CNₓ material of starting composition C₄₄N₈₆ and density 3g/cm³. Constant-temperature MD runs were performed at various temperatures and the results are summarized in Fig. 6.2.

Fig. 6.2(a) shows lifetimes of network bonds and N₂ molecules formed during 500 fs MD runs in the CNₓ sample as a function of temperature. The results show that the N₂
molecules formed are stable at significantly higher temperatures than the network bonds. This is due to the high bond energy of the triple N-N bonds. The difference of lifetimes is largest in the range 4000 - 5000 K. The network bonds are not stable in this range (the material is molten), while the lifetime of N2 molecules is comparable with the length of the MD run from the time of their formation (shown as 100 %). We note that the simulations shown here were performed with relatively high material density. This justifies the general use of our algorithm at all densities, because for lower density materials the lifetimes of N2 molecules are even higher.

Fig 6.2(b) shows the number of N2 molecules formed in the CNx sample after 200, 400 and 800 fs simulation times as a function of temperature. This result is repeated from chapter 5 for the reader's convenience. The figure clearly shows that the maximum rate of N2 formation occurs between 3000 and 6000 K, with a maximum of 19 N2 molecules formed after 800 fs at 5000 K. Note that a number of N atoms started out statistically in close proximity and these atoms tend to form N2 molecules immediately. This leads to eight N2 molecules at 1000 K where diffusion does not play a significant role. These N2 molecules are not of relevance to the temperature window, since they do not involve diffusion processes or
the release of N atoms from the network. Above 1000 K, the rate of N₂ formation steadily increases until a maximum at 5000 K is reached. Above 5000 K, the rate progressively decreases because two N atoms encountering each other are increasingly likely to carry too much thermal energy to form a stable N₂ molecule. In these simulations all N₂ molecules formed were considered to be stable, so it is possible that the real rate of the N₂ formation decreases even more at high temperatures.

Collectively, the results presented suggest that the N₂ removal run should be accomplished at temperature(s) between 4000 and 5000 K. In this range, the effective formation of relatively stable N₂ molecules has been observed, while the rest of the material is molten. Because the material is in a molten state, the final structure is not affected by replacing the exponential cooling above 3000 K by the constant temperature N₂ removal run or by length of this run.

In order to confirm the suitability of our protocol for materials other than CNₓ, 500 fs constant temperature MD runs were performed at 5000 K for samples of SiNₓ and BNₓ. These samples had the same atomic density and equivalent composition (Si₄₄N₈₆ and B₄₄N₈₆, respectively) as the previous CNₓ sample. Fig 6.3 shows for these materials similar lifetimes of N-containing bonds (including N₂ molecules), while lifetimes of the B-B and Si-Si bonds are even shorter than the lifetime of C-C bonds.

Moreover, it is revealed in Fig. 6.3 that formation of N₂ molecules in the SiNₓ material is much less intensive than in the BNₓ and CNₓ materials at the same temperature and atomic density. Only one N₂ molecule was formed during the 500 fs MD run in the Si₄₄N₈₆ sample in comparison with 13 and 17 molecules formed in the B₄₄N₈₆ and C₄₄N₈₆ samples, respectively. This illustrates the experimentally observed effect of Si to improve the retention of N in structures of N-containing materials prepared with varied Si-content²⁻⁴.

![Figure 6.3. Lifetimes of network bonds and N₂ molecules in samples of C₄₄N₈₆, B₄₄N₈₆ and Si₄₄N₈₆ during 500 fs MD runs at 5000K. Lifetimes are shown as percentages of maximum possible lifetimes (the time from the formation of the bond/molecule until the end of the simulation). Numbers of N₂ molecules formed are given in the legend.](image)
The lifetimes of Si/B/C-containing bonds at the same temperature and atomic density correlate perfectly with proportions of these bonds observed in experimentally prepared Si-B-C-N materials. It was shown in Ref. 5 by X-ray photoelectron spectroscopy that Si, B and C preferentially bond to N. The analysis also detected some C-C (and Si-C) bonds, but evidence of Si-Si and B-B bonds was not seen (note short lifetimes of these bonds in Fig. 6.3).

### 6.4 Conclusions

In MD liquid quench simulations of N-containing amorphous materials we have observed the formation of free N$_2$ molecules. In order to compensate for the loss of N atoms and still achieve a desired N-content in the quenched material, the liquid quench simulations of these materials were commenced with sufficient N-excess. We developed a modified liquid-quench algorithm in which the N$_2$ molecules are removed from simulation cell after forming. In this protocol, the high-temperature part of simulation where the material is molten and the N$_2$ molecules form is flexible in its time duration. We have shown that this $N_2$ removal run has to be accomplished between 4000 and 5000 K where the effective formation of relatively stable N$_2$ molecules has been observed, while in the rest of the material no stable network bonds form. The results also suggest that for given temperature and atomic density the rate of N$_2$-formation in Si/B/C-containing materials decreases with increasing Si-content. This explains the ability of Si to enhance the final N-content in experimentally prepared materials.

### 6.5 References

1. J. Houška et al., prepared for submitting to Molecular Simulation.
Chapter 7 - The effect of argon

7 The effect of argon on the structure of amorphous Si-B-C-N materials

This chapter is based on results published in Ref. 1. Using liquid quench simulations, we investigate here how the presence of Ar atoms in the sample affects the liquid quench and the final structure of the S-B-C-N materials. In the absence of Ar, we find that the final structures are homogeneous. The presence of Ar however leads to the formation of silicon-enriched regions in the vicinity of implanted Ar atoms. This result provides new insight into the role of implanted Ar in formation of structures in amorphous S-B-C-N materials. It also explains the ability of Si to relieve stress generated by these implanted Ar atoms.

7.1 Introduction

Since sputtering is typically performed in an Ar-containing atmosphere, materials prepared with this method are found to contain small amounts of implanted Ar atoms. These atoms arise from the impact of energetic Ar atoms or ions from the discharge or their reflection from the sputtering target\(^2\). Implantation of Ar has been correlated with the presence of compressive stress in the films\(^3,4\). It has previously been noted in the chapter 3 that the implantation of Ar atoms into amorphous S-B-C-N materials (prepared by magnetron sputtering in various N\(_2\)+Ar mixtures) leads to variations in a number of material properties; for example an increase in compressive stress. Experimental results shown in chapter 3 (figure 3.7) suggest that compressive stress created by implanted Ar atoms is more effectively relieved in S-B-C-N films with high Si-content. In the literature, little has been reported concerning the mechanism by which Ar incorporation affects structural and mechanical properties of these materials. First-principles simulations are performed in this chapter to understand these observations at an atomistic level. We discuss the structural effects of Ar on the network and how high Si content may help relieve that part of the compressive stress, which is caused by implanted Ar.

Our simulations in this chapter focus on samples of composition Si\(_{32}\)B\(_{10}\)C\(_6\)N\(_{52}\) (deposited previously with various \(U_b\) between 0 and -500 V) and Si\(_{32}\)B\(_{10}\)C\(_6\)N\(_{52}\)Ar\(_6\) (\(U_b = -500\) V). Experimentally, the stronger Ar bombardment (discharge mixture Ar/N\(_2\) = 3:1 instead of 1:1) was found to increase both the content of implanted Ar and the atomic density of the Si\(_{32}\)B\(_{10}\)C\(_6\)N\(_{52}\)Ar\(_6\) sample.

The modified liquid-quench algorithm proposed in previous chapter 6, which accounts for formation of N\(_2\) molecules during quenching, was been used for the simulations discussed in this chapter. A cooling time of 500 fs was used to simulate materials deposited with \(U_b = -500\) V, while shorter cooling times were used to simulate the effect of lower \(|U_b|\). Although all deposited samples were found to contain small amounts of hydrogen, this was not included in the simulations.
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7.2 Results

7.2.1 Simulations of material without implanted Ar

We first discuss our simulations of a sample of composition Si$_{32}$B$_{10}$C$_6$N$_{52}$ where our initial objective is to demonstrate that this composition prefers a homogeneous distribution of atoms in the network; i.e. this material does not segregate into locally distinct regions or phases. Because our simulations are run in relatively small unit cells, a demonstration of homogeneity in a network is not straightforward. This is because we have to distinguish between genuine and coincidental phase segregation; the latter refers to the situation that the initial distribution of atoms contains random inhomogeneities.

Full liquid-quench simulations of the Si$_{32}$B$_{10}$C$_6$N$_{52}$ structure were performed using exponential cooling times of 100 fs and 500 fs to simulate the effect of bias voltages $U_b$ of -100 and -500 V, respectively. A typical snapshot of the structure obtained from these simulations is shown in figure 7.1. In the upper part of the figure, we can see a region of SiN$_x$ containing no B and C atoms.

In order to quantify segregation we introduce two criteria. Since we have more than 50% N in our compositions, likely binary phases are SiN$_x$ or BN$_x$ or CN$_x$. Our first criterion to measure the presence of such phases is the percentage of N atoms bonded only to one of Si, B or C. The number of bonds between atoms of the same kind is a second criterion, which detects the existence of elemental phases (such as pure Si or C networks).

![Fig. 7.1: Snapshot from the end of the liquid quench simulation of a S-B-C-N material of composition Si$_{32}$B$_{10}$C$_6$N$_{52}$ with no Ar atoms in the structure. Large black circles are C, medium grey are N, light grey are B, white circles correspond to Si, the small black dots represent Wannier function centres (WFCs).]
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Figure 7.2 shows these criteria applied to structures prior to cooling and after cooling runs of 50, 100, 250 and 500 fs. The data shows a continuous reduction of both segregation criteria; thus, there is a general increase in structural homogeneity with increased cooling time. We conclude that the initial SiN\textsubscript{x} phase detected in the structure in figure 7.1 is the result of random clustering in the melt.

This result suggests that the Si\textsubscript{32}B\textsubscript{10}C\textsubscript{6}N\textsubscript{52} composition has a thermodynamic preference for a maximally homogeneous structure. Long cooling times occur for impacts of high energy (high |U\textsubscript{b}| such as 500 V), for which we expect materials of homogeneous structure. In materials deposited with small |U\textsubscript{b}| such as 100 V some segregated regions such as SiN\textsubscript{x} may survive.

**Fig. 7.2:** Dependence of segregation in quenched structures of composition Si\textsubscript{32}B\textsubscript{10}C\textsubscript{6}N\textsubscript{52} on the time taken to quench from 3000K to 650K. Segregation was measured using two criteria: Criterion 1 shown in (a) is the percentage of nitrogen atoms bonded to only one atom type (B, C, or Si) other than nitrogen. Criterion 2 shown in (b) is the percentage of chemical bonds between atoms of the same type. For both criteria, higher values are indicative of a less homogeneous structure. The 0 fs data point measures segregation in the molten structure prior to cooling. Subsequent data points characterize the structures just after cooling to 650K.

Figure 7.2 shows these criteria applied to structures prior to cooling and after cooling runs of 50, 100, 250 and 500 fs. The data shows a continuous reduction of both segregation criteria; thus, there is a general increase in structural homogeneity with increased cooling time. We conclude that the initial SiN\textsubscript{x} phase detected in the structure in figure 7.1 is the result of random clustering in the melt.
7.2.2 Simulations of material with implanted argon

We now examine the effect of implanted argon on the S-B-C-N network. For this purpose 6 additional argon atoms were added into the network to form the composition $\text{Si}_{32}\text{B}_{10}\text{C}_6\text{N}_{52}\text{Ar}_6$ and simulations were performed with a cooling time of 500 fs. A typical simulated structure is shown in figure 7.3. The argon atoms are not bonded into the network (note how the WFCs associated with Ar are non-bonding). Five of the six argon atoms lie close together. The non-bonding character of the Ar creates “cavities” around them.

In order to determine the effect of implanted Ar atoms on structural homogeneity, we show in figure 7.4 the distributions of the distances of Si, B, C and N atoms to the nearest Ar atom. The distribution Si-Ar is more heavily weighted to short distances than are the distributions for the other atom types, suggesting the formation of a Si-rich phase around implanted Ar atoms. The average composition of the part of the sample surrounding the implanted Ar atoms (within a radius of $\leq 3.6$ Å) is $\text{Si}_{36}\text{B}_9\text{C}_6\text{N}_{49}$, while the average composition of the rest of the sample is $\text{Si}_{24}\text{B}_{13}\text{C}_6\text{N}_{57}$. This difference can be considered significant because of the preference for a homogeneous structure in the sample without Ar, discussed in the previous section.

An explanation of this phenomenon may be that the longer and more flexible Si bonds (in comparison to B, C and especially N bonds) allow the Ar induced cavities to be accommodated into the structure with minimal energy penalty including generated stress. Covalent radii of Si, B, C and N are 1.11, 0.82, 0.77 and 0.75 Å. In our structure the calculated average bond lengths (including bonds of all orders with all species) were 1.80 for Si-containing bonds and 1.51 for all other bonds. The argon atoms sit in cavities with distances of at least 2.2 Å (lower bound of first peaks on figure 7.4) separating them from other atoms in the network. The longer bonds associated with silicon allow silicon rich regions to contain natural cavities which are larger than in silicon-poor regions. Such cavities

Fig. 7.3: Snapshot from the end of a simulation of a structure of composition $\text{Si}_{32}\text{B}_{10}\text{C}_6\text{N}_{52}\text{Ar}_6$. Large black circles are C, medium grey are N, light grey are B, white are Si and dark grey (isolated) circles correspond to Ar. The small black dots represent Wannier function centres (WFCs).
allow the incorporation of argon with minimum energy penalty. The flexibility of the long silicon containing bonds enables these bonds to deform to accommodate the argon atoms with minimal generation of stress. This explains the experimental observation (chapter 3) that compressive stress generated by implanted Ar is lowest in samples with highest silicon content.

Deeper insight into the role of Ar in determining the structure of S-B-C-N materials can be gained by calculating selected statistics. Structural statistics comparing the Si$_{32}$B$_{10}$C$_6$N$_{52}$ and Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$ samples, generated using cooling times of 500 fs (corresponding to the experimental $U_b = -500$ V), are shown in table 7.1. Table 7.1 reveals several important features of the effects of argon inclusion into the material.

**Fig. 7.4:** Distributions of distances of Si, B, C and N atoms to the nearest Ar atom in the sample Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$. Data are summarized over all atoms of the respective kind and over 69 snapshots made during the 0.5 ps production run at the end of the liquid-quench simulation. In the Si-Ar distribution a high proportion of the distances are in the lower part of the range.
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Table 7.1: Selected averaged statistics for simulated materials Si$_{32}$B$_{10}$C$_6$N$_{52}$ and Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$. The Si content percentages, given in brackets, are for the sub-set of atoms and bonds in the “vicinity” of Ar. Vicinity is defined for atoms as those which are closer than 3.6 Å to an Ar atom and bonds having an Ar atom closer than 2.5 Å (perpendicular distance).

<table>
<thead>
<tr>
<th>Quantity</th>
<th>S-B-C-N</th>
<th>S-B-C-N-Ar</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si content</td>
<td>32%</td>
<td>32% (36%)</td>
</tr>
<tr>
<td>Si-containing bonds</td>
<td>75%</td>
<td>73% (96%)</td>
</tr>
<tr>
<td>fraction of all B or C containing bonds which also include Si</td>
<td>9%</td>
<td>24% (66%)</td>
</tr>
<tr>
<td>Criterion 1 for segregation</td>
<td>43%</td>
<td>52%</td>
</tr>
<tr>
<td>Criterion 2 for segregation</td>
<td>9%</td>
<td>8%</td>
</tr>
<tr>
<td>average length - all bonds (Å)</td>
<td>1.70</td>
<td>1.72</td>
</tr>
<tr>
<td>average length - single BN (Å)</td>
<td>1.51</td>
<td>1.55</td>
</tr>
<tr>
<td>average length - single CN (Å)</td>
<td>1.41</td>
<td>1.46</td>
</tr>
<tr>
<td>number of rings</td>
<td>9.0</td>
<td>18.6</td>
</tr>
<tr>
<td>average ring size</td>
<td>5.8</td>
<td>6.0</td>
</tr>
</tbody>
</table>

- Silicon tends to accumulate in the vicinity of the Ar atoms. To show this, we use a statistic applying to the group of bonds surrounding argon atoms. These are defined as those bonds, which have a perpendicular distance of less than 2.5 Å to an argon atom. Silicon is present in 96% of these bonds whereas it is only present in 73 % and 75 % of all bonds in the argon-containing and argon-free sample, respectively.

- The presence of argon induces a major shift in the bonding preferences of all atom types. To show this we use the statistic shown in row 3 of table 7.1: fraction of all B or C containing bonds, which also include Si. B, C and Si tend to form bonds with N in the absence of argon, B exclusively whereas C and Si preferentially. This effect has also been noted in our experimental observations (Chapters 3 and 4). In the simulated Ar-containing sample the tendency for B and C to bond with Si is greatly increased. In the Ar-free sample, only 9 % of all bonds containing B or C contain Si, whereas in the Ar-containing sample 24 % of all bonds containing B or C contain Si. In the group of bonds surrounding Ar atoms, the effect is even more pronounced with 66 % of bonds containing B or C containing Si. These changes in bonding preference with the introduction of Ar are reflected in the increase in Criterion 1 as shown in row 4 of table 7.1.

- Although the Ar-containing sample is denser (smaller volume per atom), it is remarkable that the averaged bond length is larger (row 6) than that for the Ar-free sample. This is not only due to the higher total percentage of longer Si-containing bonds, but also due to the longer bonds of certain types (single BN, single CN) prevailing in the part of the sample far from the Ar atoms (rows 7 and 8). This keeps approximately the same atomic density in this part of the sample where the Si-content (and therefore the number of long Si-containing bonds) is reduced.

- Adding Ar to the sample also has a major impact on the topology of the network as revealed by the ring statistics. In the last 2 rows of table 7.1, we see that the number of rings is doubled after addition of Ar. This documents the transition from the 3D structure to the dense 2D envelopes around the Ar-containing cavities. The numbers of the rings were calculated using the algorithm of Franzblau\textsuperscript{5}.
Figures 7.5 and 7.6 show the effect of temperature on the segregation of Si around implanted Ar (larger microvoids) or He (smaller microvoids) atoms. Segregation is not stable in the molten state and is expected to occur below some temperature limit. The development of the percentage of Si around (up to 3.6 Å) Ar atoms during the liquid-quench simulation of Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$ sample is shown in figure 7.5. The trendline shows that this quantity starts to increase in the equilibration phase at the end of the cooling and increases during the equilibration until a maximum has been reached. The maximum exists because diffusion is limited once the solid has formed.

Figure 7.5 also shows the same statistic (i.e. percentage of Si around implanted inert gas atoms) in which the argon was replaced with helium. The same atomic density and cooling time have been used for this simulation. First minima of the pair correlation functions in which one of the atoms is He are around 1.9 Å in comparison with 2.2 Å for the Ar case. It suggests that the envelopes around smaller cavities containing He can be formed from all bond types rather than only from the long Si-containing bonds as in the Ar-containing structure. Thus, there isn’t any observable segregation of Si around implanted He atoms.

In order to examine the effect of equilibration temperature on segregation of Si around Ar more closely, we performed a series of constant temperature 1 ps MD runs at temperatures between 100 and 2000 K. These simulations used the (nearly homogeneous) starting structure of the previous equilibration at 650 K. The velocities were scaled in accordance with the new temperature. For all temperatures, the percentage of Si around Ar atoms increased during the first 0.5 ps of equilibration while the mean value was stable during the second 0.5 ps. Figure 7.6 shows averaged stable values of percentages of Si around Ar for all simulated temperatures.
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Fig. 7.6: Segregation of Si around implanted Ar atoms in samples of composition Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$ equilibrated at various temperatures. The vertical axis refers to the percentage of Si atoms in the group of Si, B, C and N atoms that lie in the vicinity of an Ar atom. Atoms in the vicinity are defined as those which are closer than 3.6 Å to an Ar. The data are averaged over the stable period 0.5 – 1 ps from the start of equilibration. The percentage of Si around Ar reaches a maximum for equilibration temperatures in the range 1000 - 1500 K.

equilibration temperatures. This figure also shows that for equilibration temperatures between 100 and 1000 K, the segregation of Si around Ar increases with increasing temperature. We attribute this to increasing temperature-dependent diffusion coefficients. At higher temperatures, the kinetic energies of atoms may be comparable or larger than the energy penalty associated with having the Ar cavities surrounded also by short and inflexible non-Si-containing bonds. This leads to a reduction in the degree of Si segregation around the Ar. These results lead us to predict that silicon should relax compressive stress generated in films deposited using argon sputtering more effectively at higher deposition temperatures provided that the temperature is below 1000 K.
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7.3 Conclusions

We investigated using liquid quench simulations the origin of the ability of Si to reduce the stress generated in S-B-C-N films by argon. The simulations show that S-B-C-N has a preference for a completely homogeneous structure in the absence of argon. When Ar atoms were included in the simulation, we observed the segregation of a Si-rich phase around them. We propose that the driving force for the segregation is the energy advantage gained by surrounding Ar atoms with longer and more flexible Si-containing bonds. This explains the ability of Si to inhibit the extra stress, otherwise generated by implanted Ar in S-B-C-N materials with zero or low Si content.

The incorporation of argon in the simulations caused major changes in the bonding preferences of all the atoms in the network. For example, all atoms showed a preference for bonding to nitrogen in the absence of Ar, whereas they showed a general increase in bonding to silicon when argon is present.

Based on the simulations, we make the prediction that the effectiveness of silicon to relieve stress in S-B-C-N films sputtered in argon will increase with deposition temperature up to approximately 1000K.

7.4 References

8 Comparison of measured and calculated characteristics of Si-B-C-N materials and the role of individual elements in them

This chapter compares characteristics of the simulated networks with related experimental results. They are compared in order to explain the experimental results where possible, and to show the power and limits of the simulation method used. The chapter is divided into sections focusing on:

2. Characteristics related to hardness.
3. Thermal stability.
4. Optical conductivity and band gap.

8.1 Structural and bonding data

In this section, various structural and bonding data are shown and discussed. Simulations were performed for samples of compositions:

- $\text{Si}_{32}\text{B}_8\text{C}_6\text{N}_{54}$ and $\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}$: representing typical compositions deposited with various sputtered targets.
- $\text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6$ ($U_b = -100 \text{ V}$) and $\text{Si}_{33}\text{B}_6\text{C}_{13}\text{N}_{46}\text{Ar}_2$ ($U_b = -500 \text{ V}$): representing similar compositions deposited with same sputtered target and different substrate bias voltage, $U_b$.

8.1.1 Related theory - calculation of bulk modulus

In 1985 Cohen published the following empirical formula which describes very well the dependence of bulk modulus $B$ on averaged coordination number $N_c$, bond length $a_0$ and bond ionicity $\lambda$:

$$B = \frac{(1971 - 220\lambda)a_0^{-3.5}}{(N_c)}$$ (Eq. 8.1)

Although the formula was primarily derived for crystalline materials, qualitative predictions based on differences in $N_c$, $a_0$ and $\lambda$ can be made also for amorphous materials.

While $N_c$ and $a_0$ can be directly calculated from the simulated network structures, $\lambda$ is to be derived from positions of Wannier function centres, which define the bonds. We simulated networks of several known crystalline materials containing elements from the IVA group (cubic and wurzite SiC) and IIIA + VA group (cubic and wurzite BN, cubic AlP and wurzite AlN) and observed the quantity $\Lambda = d_1r_2/d_2r_1$. Here, $d_{1(2)}$ are distances of the first(second) atom from the Wannier centre defining the bond between them, and $r_{1(2)}$ are covalent radii of the atoms.

<table>
<thead>
<tr>
<th>material</th>
<th>$\lambda$</th>
<th>$\Lambda$</th>
</tr>
</thead>
<tbody>
<tr>
<td>c-SiC</td>
<td>0</td>
<td>1.32</td>
</tr>
<tr>
<td>w-SiC</td>
<td>0</td>
<td>1.28</td>
</tr>
<tr>
<td>c-BN</td>
<td>1</td>
<td>1.73</td>
</tr>
<tr>
<td>w-BN</td>
<td>1</td>
<td>1.69</td>
</tr>
<tr>
<td>c-AlP</td>
<td>1</td>
<td>1.69</td>
</tr>
<tr>
<td>w-AlN</td>
<td>1</td>
<td>1.97</td>
</tr>
</tbody>
</table>

Table 8.1: Ionicities of bonds in materials according to Cohen’s definition ($\lambda$) and to positions of calculated Wannier function centres ($\Lambda = d_1r_2/d_2r_1$).
In order to calculate the bond ionicity $\lambda$, we use a simple linear relation between $\lambda$ and $\Lambda$: 

$$\lambda = \frac{(\Lambda - 1)}{(\Lambda_0 - 1)}$$  \hspace{1cm} (Eq. 8.2) 

According to the averaged results summarized in table 8.1 we set $\Lambda_0 = 1.7$. This formula gives the following results, in agreement with Cohen's definition (1,2) or experimental experience (3):

(1) $\lambda = 0$ for purely covalent homonuclear bonds (i.e. with a Wannier centre exactly in the middle of the bond).

(2) $\lambda \approx 1$ for bonds between elements from IIIA and VA group.

Fig. 8.1: Snapshots from the liquid-quench simulation of a Si-B-C-N material of composition Si$_{32}$B$_8$C$_6$N$_{54}$ (panel a) and Si$_{11}$B$_{14}$C$_{39}$N$_{36}$ (panel b). Large black circles are C, dark grey are N, light grey are B, white circles correspond to Si, the small black dots represent Wannier function centres (WFCs).
(3) $\lambda \cong 0.4$ for bonds in Si-C which is a group-IVA material, but partially ionic and often considered (c-SiC) to be part-way between a group-IV covalent and an III-V ionic semiconductor\(^1\).

### 8.1.2 Bonding statistics as a function of elemental composition

Typical Si-B-C-N structures that are obtained at the end of the exponential cooling and subsequent equilibration runs are shown in Figs. 8.1(a) - composition Si\(_{32}\)B\(_8\)C\(_6\)N\(_{54}\) and 8.1(b) - Si\(_{11}\)B\(_{14}\)C\(_{39}\)N\(_{36}\). There is a prevalence of single bonds in the high-Si/C composition (Fig. 8.1(a)) structure compared to the low-Si/C composition (Fig. 8.1(b)) structure, where there are many more double bonds and also number of triple (C≡N) bonds.

Another phenomenon that can be observed in Fig. 8.1 is that the position of bonding Wannier function centres (WFCs) is often far from geometrical centre of the bond. In particular, positions of WFCs in Si-containing bonds (with atoms other than Si) are far from Si atoms (more than what would be expected due to the higher covalent radius of Si) and close to the other atoms. On the contrary, the WFCs are often close to N in the N-containing bonds. Both of these phenomena are illustrated in tables 8.2 and 8.3.

<table>
<thead>
<tr>
<th>atom pair</th>
<th>bonds in Si(_{32})B(_8)C(<em>6)N(</em>{54})</th>
<th>bonds in Si(<em>{11})B(</em>{14})C(<em>{39})N(</em>{36})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si Si</td>
<td>1.7 0.0 0.0</td>
<td>1.0 0.0 0.0</td>
</tr>
<tr>
<td>Si B</td>
<td>1.0 0.0 0.0</td>
<td>0.0 0.0 0.0</td>
</tr>
<tr>
<td>Si C</td>
<td>3.0 0.0 0.0</td>
<td>11.2 0.0 0.0</td>
</tr>
<tr>
<td>Si N</td>
<td>110.6 7.4 0.2</td>
<td>30.1 0.6 0.0</td>
</tr>
<tr>
<td>B Si</td>
<td>1.0 0.0 0.0</td>
<td>0.0 0.0 0.0</td>
</tr>
<tr>
<td>B B</td>
<td>0.0 0.0 0.0</td>
<td>0.0 0.0 0.0</td>
</tr>
<tr>
<td>B C</td>
<td>0.0 0.0 0.0</td>
<td>16.3 0.0 0.0</td>
</tr>
<tr>
<td>B N</td>
<td>14.0 9.0 0.0</td>
<td>22.1 7.3 0.0</td>
</tr>
<tr>
<td>C Si</td>
<td>3.0 0.0 0.0</td>
<td>11.2 0.0 0.0</td>
</tr>
<tr>
<td>C B</td>
<td>0.0 0.0 0.0</td>
<td>16.3 0.0 0.0</td>
</tr>
<tr>
<td>C C</td>
<td>0.0 1.0 0.0</td>
<td>17.4 9.8 0.0</td>
</tr>
<tr>
<td>C N</td>
<td>4.0 6.2 0.8</td>
<td>22.4 8.4 4.4</td>
</tr>
<tr>
<td>N Si</td>
<td>110.6 7.4 0.2</td>
<td>30.1 0.6 0.0</td>
</tr>
<tr>
<td>N B</td>
<td>14.0 9.0 0.0</td>
<td>22.1 7.3 0.0</td>
</tr>
<tr>
<td>N C</td>
<td>4.0 6.2 0.8</td>
<td>22.4 8.4 4.4</td>
</tr>
<tr>
<td>N N</td>
<td>2.0 0.0 0.0</td>
<td>1.0 0.0 0.0</td>
</tr>
</tbody>
</table>

Table 8.2: Bonding statistics of simulated Si-B-C-N samples of compositions Si\(_{32}\)B\(_8\)C\(_6\)N\(_{54}\) and Si\(_{11}\)B\(_{14}\)C\(_{39}\)N\(_{36}\). Data are averaged over 69 snapshots collected during a 0.5 ps production run.

Table 8.2 includes complete bonding statistics for the Si-B-C-N samples of compositions Si\(_{32}\)B\(_8\)C\(_6\)N\(_{54}\) and Si\(_{11}\)B\(_{14}\)C\(_{39}\)N\(_{36}\) studied. The non-integer numbers result from averaging of the results over 69 snapshots collected during 0.5 ps production runs. Numbers of bonds of same kind and order change not only due to the bond-breaking processes (relatively rare at the low temperatures of production runs), but also due to the converting of a bond between permanently bonding atoms from double to single/triple state and vice versa.
The flipping process during which a bonding WFC alternates between two different atom pairs is discussed in detail in Ref. 3.

The table 8.2 shows that the most populated bonds in the high-Si/C composition are Si-N (mostly single), followed by B-N (single and double) and C-N (all bond orders). In the low-Si/C composition, other bond kinds have to be taken into account: C-Si (single), C-B (single) and C-C (single and double). The higher preference of carbon (in comparison with silicon) to form double and triple bonds leads to lower coordination numbers of sp²- and sp³-hybridised C atoms and therefore to lower bulk moduli (which indicates lower hardness) of the low-Si/C Si-B-C-N materials. The phenomena shown are in accordance with experimental observations (see measurements of hardness and bonding structure in chapter 3). Note that longer Si-containing bonds in the high-Si/C composition would on the contrary decrease the bulk modulus (B \sim 1/d^{3.5} in the Cohen's formula for crystalline materials), but according to the experimental results the dependence of B on d is much weaker in amorphous materials.

### 8.1.3 Elemental bonding trends explained in terms of valence electrons and electronegativity

Table 8.3: Structural characteristics of simulated Si-B-C-N samples of compositions \( \text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54} \) and \( \text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36} \). Data are averaged over 69 snapshots collected during a 0.5 ps production run. Part (a) shows averaged coordination numbers of the atoms of each element. Part (b) shows averaged atomic charges (in e) and their standard deviations for atoms of each element, together with their electronegativities.

Table 8.3(a) shows the bonding behaviour of element in terms of their averaged coordination numbers. Table 8.3(b) shows averaged charges of atoms of the constituent elements, together with values of their Pauling electronegativity².

- The average coordination number of Si, which has 4 valence electrons and forms mainly single bonds, is close to 4. The average charge on Si atoms is positive at around 0.25e. This is in accordance with its relatively low electronegativity, confirmed also by the observed tendency of WFCs (negatively charged electron pairs) in Si-containing bonds to be far from the Si atoms (see Fig. 8.1).
- The average coordination number of B (with 3 valence electrons) is close to 3 despite the number of double B=N bonds, which increases the number of bonding electrons associated with B atoms to over 3. The boron atomic charge is nevertheless close to zero due to the strongly ionic character of B-N and especially B=N bonds (where both WFCs are close to the N atom).
The average coordination number of C, with 4 valence electrons, is around 3 due to the number of double and triple C-containing bonds. The average charge on the C atoms is close to zero as it is for B, but the deviation is significantly higher (the highest of all atom types). This is due to two different "ionicity directions" of C-containing bonds (the WFCs are closer to C in bonds with Si and B and far from C in bonds with N). The wide range of hybridisations (number of associated WFCs) adopted by C is another reason for the large fluctuations in charge on the carbon atoms. An extreme example of this is a carbon atom associated with 6 WFCs which form 2 C≡N bonds (see top part of Fig. 8.1(b)), which has however one of the highest positive carbon charges of 0.129e because all 6 WFCs are far from the C atom and close to the respective N atoms.

The average coordination number of N, with 5 valence electrons, is slightly less than 3. This is due to the fact that most of N atoms are associated with one non-bonding WFC (*lonepair*), which reduces averaged number of bonding WFCs associated with N atoms to 3. The average charges on N atoms are negative. The total negative charge on all N atoms is close to the total positive charge on all the Si atoms. This is in accordance with N having the highest relative electronegativity, illustrated also by the proximity of WFCs to N atoms in the N-containing bonds (with atoms other than N).

Table 8.4 includes exact ionicities of all bonds with non-negligible population in at least one of all simulated Si-B-C-N samples. It was found that their averaged values do not depend significantly on sample composition. The most significant findings are:

- behaviour of the atoms is in agreement with their electronegativities (see table 8.3).
- the homonuclear bonds are not exactly covalent in amorphous materials: \( \lambda = 0.1-0.3 \).
- ionicities of heteronuclear single bonds are in the range \( \lambda = 0.4-1.0 \).
- ionicities of heteronuclear double bonds are in the range \( \lambda = 1.0-2.0 \).
- ionicities of all double bonds are higher than ionicities of equivalent single bonds.
• in accordance with the definition of $\lambda$, the single and double B–(=)N bonds (elements from IIIA and VA group) are the most ionic of all single (double) bonds, followed closely by the Si–(=)N bonds. The C-containing bonds have relatively low ionicities, but the effect which this should have of increasing bulk modulus will be offset by the high proportion of double and even triple C-containing bonds.

8.1.4 Bonding statistics as a function of $U_b$

(a) Sample | coord. Si | coord. B | coord. C | coord. N
---|---|---|---|---
$\text{Si}_{31}\text{B}_8\text{C}_{13}\text{N}_{46}\text{Ar}_2$ [-100 V] | 3.90 | 3.24 | 3.03 | 2.82
$\text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6$ [-500 V] | 3.85 | 3.10 | 3.03 | 2.79

(b) Sample | coord. bond length (Å) | our ionicity $\Lambda$ | Cohen's ionicity $\lambda$
---|---|---|---
$\text{Si}_{31}\text{B}_8\text{C}_{13}\text{N}_{46}\text{Ar}_2$ [-100 V] | 3.22 | 1.7454 | 1.56 | 0.80
$\text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6$ [-500 V] | 3.18 | 1.7311 | 1.64 | 0.91

effect on B (%) | 1.1 | -2.9 | 1.4

Table 8.5: Structural characteristics of simulated Si-B-C-N samples of compositions $\text{Si}_{31}\text{B}_8\text{C}_{13}\text{N}_{46}\text{Ar}_2$ ($U_b = -100$ V) and $\text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6$ ($U_b = -500$ V). Part (a) shows changes in averaged coordination numbers of individual atoms. Part (b) shows changes in averaged total coordination number (without Ar), bond length and bond ionicity, and effect of these changes on bulk modulus using Cohen's formula for crystalline materials.

Table 8.5 quantifies the effect of observed structural characteristics on bulk moduli of $\text{Si}_{31}\text{B}_8\text{C}_{13}\text{N}_{46}\text{Ar}_2$ (deposited with $U_b = -100$ V which led to relatively low content of implanted Ar; simulated with cooling time of 100 fs) and $\text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6$ (deposited with $U_b = -500$ V which led to relatively high content of implanted Ar and to decreased C content due to the stronger sputtering of loosely bounded C-N compounds$^{4,5}$; simulated with cooling time of 500 fs).

Table 8.5(a) shows that the averaged coordination numbers of all atoms except carbon increase at shorter cooling time (lower $|U_b|$ and consequently lower Ar content). The coordination number of carbon is unaffected. The increase is most significant for boron, which correlates with experimentally predicted existence of an energy window for preferential formation of B(sp$^3$)-N bonds at low $|U_b|$ in BN$^6$ and Si-B-C-N (see chapter 4) materials.

Table 8.5(b) shows the effect of substrate bias (and consequent Ar content) on total averaged coordination number, bond length and bond ionicity. It can be seen that:

- the material prepared with lower $|U_b|$ possesses higher total averaged coordination number and lower averaged bond ionicity (see generally lower ionicities of single bonds in table 8.4). This would be expected to have a positive effect on its bulk modulus.
- because single bonds are always longer than equivalent double bonds, it can be seen that in the low $|U_b|$ material the averaged bond length is higher. This would be expected to have a negative effect on its bulk modulus.
- the last row of table 8.5 shows that according to the Cohen's formula, individual effects of all discussed structural differences on bulk modulus are up to 3%, and collectively their effect is close to zero. Note that the formula used was developed for
a particular class of crystalline material and can therefore provide only a rough guide for amorphous materials. However, it is clear that calculated structural differences (despite significant differences in cooling times used and numbers of implanted Ar atoms considered) cannot fully explain the experimentally observed differences in mechanical properties of these materials of similar Si-B-C-N compositions deposited under different conditions.

8.1.5 Conclusions

The most populated bonds in the high-Si/C composition structures were found to be Si-N (mostly single), B-N (single and double) and C-N (all bond orders). In the low-Si/C composition structures, other bond types: C-Si (single), C-B (single) and C-C (single and double) also become significant.

A method to calculate bond ionicities, $\lambda$, using WFCs was developed. Typical values were 0.1-0.3 for homonuclear bonds, 0.4-1.0 for heteronuclear single bonds and 1.0-2.0 for heteronuclear double bonds. According to the experimental results, the coordination numbers (higher for Si than for C) have a more significant effect on the hardness of materials of different Si-B-C-N composition than do the bond lengths and ionicities.

A simulated sample deposited with low $|U_b|$ possessed higher averaged total coordination number at lower bond ionicity and higher bond lengths than the equivalent high $|U_b|$ simulated structure. Quantitatively, differences in these quantities alone cannot explain the experimentally observed differences in mechanical properties of these samples of similar Si-B-C-N composition.
8.2 Hardness

Section 8.1 showed that differences in quantities such as coordination number or bond ionicity cannot fully explain differences in hardness of materials of similar elemental compositions deposited in various N₂-Ar gas mixtures or with different values of substrate bias. In this section we show that variations in the amount of implanted Ar could be responsible for the differences in hardness. The amount of implanted Ar depends both on the N₂-Ar gas mixture and the bias \( U_b \), while, for example, the densification of material due to an ion bombardment takes place at any gas mixture composition. Simulations were performed for samples of compositions:

- \( \text{Si}_{32}\text{B}_{10}\text{C}_6\text{N}_{52}\text{Ar}_6 \) (\( U_b = -500 \text{ V} \), result is repeated with new comments from the previous chapter 7).
- \( \text{Si}_{31}\text{B}_8\text{C}_{13}\text{N}_{46}\text{Ar}_2 \) (\( U_b = -100 \text{ V} \)) and \( \text{Si}_{31}\text{B}_8\text{C}_9\text{N}_{46}\text{Ar}_6 \) (\( U_b = -500 \text{ V} \)).

8.2.1 An explanation for enhanced hardness based on simulations

Although there is no method available for the direct calculation of hardness, structural phenomena potentially affecting the hardness can be examined. In particular, Fig. 8.2 compares segregation of Si around implanted Ar atoms in a sample of composition \( \text{Si}_{32}\text{B}_{10}\text{C}_6\text{N}_{52}\text{Ar}_6 \) (panel (a) - see the discussion in the previous chapter 7) with the hardness of three Si-B-C-N samples of similar compositions after their annealing and cooling down to the room temperature. All three samples shown in Fig. 8.2(b) were deposited at high Ar content in a N₂-Ar gas mixture (1:3), which led to relatively high contents of implanted Ar. The other deposition conditions were \( \text{C}_{20}\text{Si}_{60}\text{B}_{20} \) sputtered target, \( U_b = -100 \text{ V} \) and \( T_s = 350^\circ\text{C} \) (squares), \( \text{C}_5\text{Si}_{75}\text{B}_{20} \) sputtered target, \( U_b = -100 \text{ V} \) and \( T_s = 350^\circ\text{C} \) (circles) and \( \text{C}_5\text{Si}_{75}\text{B}_{20} \) sputtered target, \( U_b = U_f \) and \( T_s \leq 190^\circ\text{C} \) (triangles).

Segregation of Si around implanted Ar atoms leads to the formation of a sort of two-phase material, consisting of amorphous Si-rich and Si-poor regions. We believe that this can lead to an increase in the extrinsic hardness, in the same way as described previously for mixtures of two nanocrystalline or nanocrystalline and amorphous materials (see, for example, Ref. 7). It can be seen in Fig. 8.2 for all three samples shown that the "extra hardness" which the material obtains (or loses) due to the annealing has entirely the same temperature dependence as the segregation of Si around Ar, which takes place due to its activation at high temperatures. These results collectively suggest that annealing of Si-B-C-N materials containing implanted Ar can lead to changes in their hardness due to the segregation of Si around the Ar-containing cavities. This increases with temperature up to 1000 K, and then starts to decrease above 1500 K where high kinetic energies start to inhibit a stable segregation (see the discussion in previous chapter 7).
Figure 8.3 shows the segregation phenomenon in detail for two samples with different Ar contents of 2 and 6% (this is the same pair of samples which was used for examining of the effect of $U_b$ in the previous section 8.1). The samples are Si$_{31}$B$_8$C$_9$N$_{46}$Ar$_2$ (deposited with $U_b = -100$ V) and Si$_{31}$B$_8$C$_9$N$_{46}$Ar$_6$ (deposited with $U_b = -500$ V). In the sample containing 6% Ar, shown on the right side of Fig. 8.3, most of the network atoms have at least one implanted Ar atom at a distance of $\leq 4$ Å (upper bound of first peaks of the dependences - the limit is slightly higher than 3.6 Å in the previous chapter probably due to a different atomic density). In contrast, in the sample containing 2% Ar, shown on the left side of the figure, the distances to the nearest Ar atom span a wide range with most distributions showing several comparable peaks up to the maximum possible distance imposed by the periodic simulation cell.

We define the Si-rich regions (in close proximity to Ar atoms) as those which consist of atoms in the first peaks in Fig. 8.3, they fill space between two concentric spheres of radii 2.5 and 4 Å around each implanted Ar atom (space around each Ar atom up to approximately 2.5 Å is empty according to Fig. 8.3). The spheres can of course intersect especially at high Ar

\[ \text{Fig. 8.2: Panel (a) (repeated from the previous chapter 7 for reader's convenience) shows segregation of Si around implanted Ar atoms in samples of composition Si$_{32}$B$_{10}$C$_6$N$_{52}$Ar$_6$ equilibrated at various temperatures. The vertical axis refers to the percentage of Si atoms in the group of Si, B, C and N atoms that lie in the vicinity of an Ar atom. Panel (b) shows dependence of hardness of three Si-B-C-N films (of similar compositions as the simulated one), measured after annealing and cooling back to the room temperature, as a function of the annealing temperature.} \]
content. The rest of the sample constitutes the Si-poor matrix (away from the Ar atoms). In the 6% Ar sample, because of the high density of Ar, most of the constituent atoms are included in “high-Si” regions in close proximity to Ar (where therefore the Si content can not be increased very much). This results in an almost homogenous material. In the 2% Ar sample, the Ar density is low enough to allow segregation into close-to-Ar Si-rich regions and far-from-Ar Si-poor regions. The proportions of these two different composition zones are fairly balanced, suggesting the formation of a true heterogeneous material.

<table>
<thead>
<tr>
<th>sample composition</th>
<th>composition of regions</th>
<th>ratio of regions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si$<em>{31}$B$<em>8$C$</em>{13}$N$</em>{46}$Ar$_2$ (low $</td>
<td>\langle\rangle</td>
<td>$)</td>
</tr>
<tr>
<td></td>
<td>rest: Si$<em>{28}$B$</em>{10}$C$<em>{16}$N$</em>{49}$</td>
<td>58.3 %</td>
</tr>
<tr>
<td>Si$_{31}$B$_8$C$<em>9$N$</em>{46}$Ar$_6$ (high $</td>
<td>\langle\rangle</td>
<td>$)</td>
</tr>
<tr>
<td></td>
<td>rest: Si$<em>{22}$B$</em>{12}$C$<em>{10}$N$</em>{56}$</td>
<td>9.9 %</td>
</tr>
</tbody>
</table>

**Table 8.6:** Column 2 shows compositions of regions, which result from segregation of Si in vicinity of implanted Ar in Si$_{31}$B$_8$C$_{13}$N$_{46}$Ar$_2$ and Si$_{31}$B$_8$C$_9$N$_{46}$Ar$_6$ structures. Column 3 shows the relative sizes of the regions (in proportion of atoms included). Atoms in the vicinity of an Ar atom are defined to be those which are closer than 4 Å to an Ar atom.
The ideas presented above are quantified in Table 8.6. The table confirms that:

- In the 2%-Ar sample, comparable numbers of all network atoms are included in the close-to-Ar and far-from-Ar zones (42 and 58%, respectively). The Si enrichment around Ar atoms is consequently relatively high in comparison with the other sample.
- In the 6% Ar sample, 90% of all network atoms are included in the close-to-Ar zones. The Si-enrichment is therefore relatively low there, despite significant reduction of Si-content in the far-from-Ar rest of the sample.

Figure 8.4 contains schematic diagrams of the structures with 2% Ar and 6% Ar to illustrate the segregation concepts discussed above. The dark grey tone represents regions with higher Si. The left side of Fig. 8.4 shows the situation in the sample with 2% of implanted Ar. The dark-grey halos represent spheres containing atoms in close proximity to Ar with a silicon content of 37%, while the light-grey matrix depicts the atoms in the far-from-Ar zone which has a silicon content of 28%. On the right side of Fig. 8.4, the middle-grey halos represent spheres around implanted Ar atoms, with 34% silicon content, in the far-from-Ar white matrix with only 22% silicon content. The figure is simplified by the assumption that all Ar atoms considered lie in a plane parallel to the plane of the figure, which leads to unified halo radii. Ratios of dark and light areas in both figures refer to calculated ratios of close-to-Ar and far-from-Ar zones in both samples (42:58 and 90:10, respectively), in order to demonstrate difference between the two structures (heterogenous 2%-Ar materials on the left, almost homogenous 6%-Ar material on the right).

Fig. 8.4: A schematic diagram based on the simulations of structures of the samples Si₃₁B₈C₁₃N₄₆Ar₂ (left) and Si₃₁B₈C₉N₄₆Ar₆ (right). Darker gray tones represent higher Si content in the respective zone of a material. The halos refer to spheres with an Ar atom in the middle (r ≅ 4 Å) with enhanced Si content. Ratios of dark and light areas in both figures approximately correlate to calculated ratios of the sizes of close-to-Ar and far-from-Ar zones in both samples (42:58 and 90:10, respectively)
Chapter 8 - Comparison of experiment and simulation

Figure 8.5 demonstrates the effect of the phenomenon described above on the relative hardnesses of the samples with 2% Ar and 6% Ar. For simplicity, we assume in the figure that the Si-rich and Si-poor zones have the same values of hardness in both samples. The curve depicted in figure 8.5 is based on the finding that the hardness of a mixture of nanograin of two materials is at their proper ratio higher than the hardnesses of both constituents even when they are significantly different. Furthermore, it is considered in Fig. 8.5 that the dependence of hardness of the mixture of the Si-rich and Si-poor regions on their volume ratio is roughly symmetrical, having a maximum value at a ratio of 50%:50%. The 42%:58% ratio calculated for the 2% Ar material (see table 8.6) leads to significantly higher extrinsic hardness than the 90%:10% ratio calculated for the 6% Ar material.

8.2.2 Supporting experimental results

In this subsection, our conclusion concerning the effect of the implanted Ar concentration and the segregation of Si around Ar on hardness is examined in the light of two additional experimental results. These results show that both the silicon content (Fig. 8.6) and the argon content (Fig. 8.7) are important for the hardening of the in Si-B-C-N materials.

Figure 8.6 shows the effect of deposition temperature on hardness at various sputtered target compositions. Two series of (Si)-B-C-N samples were deposited using the B₄C-Si target at substrate temperatures Tₛ = 700 °C and Tₛ < 190 °C (no ohmic heating). The other deposition conditions were 25% N₂ + 75% Ar gas mixture and U_b = -100 V. Absolute values of the hardness of the samples are shown in figure 8.6(a), hardness differences caused by increases in Tₛ from less than 190 to 700 °C are shown in figure 8.6(b). It can be seen that while this difference is negative (that is, samples deposited with lower Tₛ are harder) at zero or low Si fraction in erosion target area, it increases almost linearly with increasing Si fraction in erosion target area over the whole range observed, becoming positive when the Si fraction is above ~30%. Then slope of the increase caused by Tₛ is approximately (11 GPa) / (75% Si in erosion target area)(500°C) ≅ 0.3 MPa per 1°C and 1% Si in erosion target area.
The figure 8.6 can be understood taking into account that the physical processes determining hardness are different for films with low Si content compared to those with high Si content. In the first case, when Si content is low, the compressive stress caused by implanted Ar atoms cannot be relaxed by segregation of Si around them and films deposited at low temperatures show high intrinsic stress and this compressive stress leads to high values of hardness. The intrinsic stress can be relieved by atomic rearrangement if deposition is carried out at elevated temperature \((T_s = 700 \degree C)\). With increasing Si content, the thermally activated stress relaxation becomes less important because the compressive stress caused by implanted Ar is relieved by segregation of Si around Ar. The main process increasing material hardness at high Si content is therefore the segregation of the material into nanoscale regions of two phases. This thermally activated segregation process is naturally more significant at higher \(T_s\) (up to \(~1000K\), as shown previously), and at higher Si content in materials and it leads to an increase in hardness with deposition temperature at high Si content.

![Graph](image)

**Fig. 8.6:** Panel (a) shows hardness of Si-B-C-N samples deposited using a \(B_4C\)-Si sputtered target at high substrate temperature \(T_s = 700 \degree C\) (full symbols) and low \(T_s < 190 \degree C\) (no ohmic heating - empty symbols). The other deposition conditions were 25% \(N_2\) + 75% \(Ar\) gas mixture and \(U_b = -100\ V\). Panel (b) shows differences of values shown in panel (a): hardness at \(T_s = 700 \degree C\) - hardness at \(T_s < 190 \degree C\). The line is a fit from linear regression.
Figure 8.7 shows the hardness as a function of Ar content in the gas mixture for two series of Si-B-C-N sample, deposited at $U_b = -100$ and -500 V with sputtered target composition $(B_4C)_{25}Si_{75}$ and substrate temperature $T_s = 350^\circ$C. Absolute values of the hardness are shown in figure 8.7(a), while hardness differences caused by change of $U_b$ from -500 V to -100 V are shown in figure 8.7(b). It can be seen that while this difference is negative (that is, samples deposited with $U_b = -500$ V are harder) at zero or very minor Ar fraction in the gas mixture, it increases almost linearly with increasing Ar fraction in the gas mixture over the whole range observed, becoming positive at the 25% $N_2 + 75\%$ Ar gas mixture composition. The slope of the increase caused by $U_b$ is thus approximately $(15 \text{ GPa}) / (75\% \text{ Ar in gas mixture})(400 \text{ V}) \approx 0.5 \text{ MPa per 1 V and 1\% Ar in gas mixture}$. Although this phenomenon was not so pronounced for samples deposited with the C-Si-B target (see chapter 3), it has been observed for all other $(B_4C)_xSi_{(100-x)}$ targets used at $x > 0$. On the contrary, the difference between hardness values at $U_b = -100$ and -500 V was almost constant at $x = 0$ (B-C-N samples).

![Graph](image_url)

**Fig. 8.7:** Panel (a) shows hardness of Si-B-C-N samples deposited using a $B_4C$-Si sputtered target at substrate bias $U_b = -100$ V (full symbols) and $U_b = -500$ V (empty symbols). The other deposition conditions were $(B_4C)_{25}Si_{75}$ sputter target and substrate temperature $T_s = 350^\circ$C. Panel (b) shows differences of values shown in panel (a): hardness at $U_b = -100$ V - hardness at $U_b = -500$ V. The line is a fit from linear regression.
The figure 8.7 can be understood taking into account that physical processes affecting material hardness are different at zero and at high Ar content in gas mixture (and therefore in deposited materials). In the first case, the hardness is higher for materials deposited at $U_b = -500$ V, possibly due to stronger bombardment by nitrogen ions which leads to ion-induced knock-on subplantation of other film-forming particles, resulting in densification of the deposited materials. The same behaviour was observed also for other amorphous materials such as $\text{CN}_x^8$ prepared in pure $\text{N}_2$. As can be seen in Fig. 8.7, the successive increase of material hardness with increasing Ar fraction in gas mixture (shown also in chapter 3) is much more pronounced at $U_b = -100$ V than at $U_b = -500$ V. Thus films deposited with high Ar fraction in gas mixture have higher hardness at $U_b = -100$ V than at $U_b = -500$ V (see also results in chapter 4). Our simulations indicate that the level of Ar incorporation in the films at high bias is too high to allow substantial Si segregation. Optimum segregation is facilitated for a few percent Ar incorporation as found in films deposited with -100V bias. The fact that this phenomenon was not observed for B-C-N materials with 0% Si content, supports the idea that the segregation of Si around Ar is responsible for the hardness enhancement in this case.

As formulated in the previous subsection 8.2.1., in the 6% Ar sample most of the atoms are included in the high-Si regions which leads to the formation of almost homogenous material, while in the 2% Ar sample, percentages of close-to-Ar Si-rich regions and far-from-Ar Si-poor regions are more balanced, suggesting formation of a true heterogenous material. Moreover, multiple thermal spikes melting the material (see in chapter 4 ~5 times higher [bombarding ions]/[film-forming particles] flux ratio at $U_b = -500$ V) can interrupt the segregation processes which take place during material equilibration (see chapter 7) and thus make any stable segregation more difficult.

8.2.3 Conclusions

Structures of samples deposited in an Ar-containing gas mixture at various $U_b$ were examined by simulations. Analysis of the simulation results was focused on the formation of Si-rich regions around implanted Ar atoms. It was found that the 6% Ar sample ($U_b = -500$ V) is not far from homogenous (most of the network atoms are close to at least one Ar), while the 2% Ar sample ($U_b = -100$ V) is heterogenous, with similar amounts of the close-to-Ar Si-rich regions and far-from-Ar Si-poor regions. This may lead to higher extrinsic hardness of the material deposited at lower $|U_b|$. The prediction was successfully tested against several experimental results.
8.3 **Temperature stability**

This section is based on results included in Ref. 9. Temperature stability of Si-(B)-C-N materials is examined by calculations of rate of N\(_2\) formation and by calculations of bond lifetimes. Simulations were performed for samples of compositions:

- \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}\) and \(\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}\) (to examine the effect of Si/C ratio on bond lifetimes).
- \(\text{Si}_{11}\text{C}_{53}\text{N}_{36}\) and \(\text{Si}_{32}\text{C}_{14}\text{N}_{54}\) (to examine the effect of B on bonding and structural data, compared with the previous pair).
- \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{44}\) and \(\text{Si}_{11}\text{C}_{53}\text{N}_{44}\) (to examine the effect of B on rate of N\(_2\) formation - same compositions were used for liquid quench simulations of samples \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}\) and \(\text{Si}_{11}\text{C}_{53}\text{N}_{36}\)).
- \(\text{Si}_{39}\text{B}_{14}\text{C}_{11}\text{N}_{44}\) and \(\text{Si}_{53}\text{C}_{11}\text{N}_{44}\) (to examine the effect of Si/C ratio on rate of N\(_2\) formation - fictitious pair of structures, obtained from the previous pair by replacing C by Si and vice versa).

8.3.1 **Bond lifetimes**

<table>
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<tr>
<th>bond type</th>
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<th>lifetimes at 2400 K (snapshots)</th>
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<td>(%)</td>
<td>(%)</td>
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</table>

*Table 8.7: Lifetimes of bonds during 500 fs MD runs in low-Si/C sample of composition \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}\), and in high-Si/C sample of composition \(\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}\). Lifetimes are given in snapshots between forming and breaking of the bond (max. 138 snapshots with 3.6 fs interval between them), and as a percentage of the simulation time remaining after formation of the bond until end of the MD run. Only the most populated bonds are included.*

Table 8.7 shows lifetimes of bonds during 500 fs MD runs in a low-Si/C sample of composition \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}\), and in a high-Si/C sample of composition \(\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}\). Only the most populated bonds were considered in order to obtain statistically significant results: these being Si/B/C-N bonds in both samples, and Si/B/C-C bonds in the low-Si/C sample only. Lifetimes were examined at a relatively low temperature of 1000 K, and at a high temperature of 2400 K which is close to the highest reported thermal stability of Si-B-C-N materials (see chapter 1 and references therein). Conversion of a double or triple bond to a bond of lower order was not considered as breaking of that bond. Because the lifetimes of all bonds are artificially limited by the finite duration of the MD run, the results will generally be too low when given in fs, and too high when given as percentages of the simulation time remaining until the end of the MD run (especially for bonds formed short time before the end of the MD run). Nevertheless, both of these results, included in table 8.7, show the same trends.
The following can be deduced from the data in table 8.7:

- Bond lifetimes at same temperature are significantly higher for the high-Si/C material than for the low-Si/C material. This not only correlates with the previously observed higher thermal stability of the high-Si/C Si-B-C-N materials\(^5\), but the significance of the difference indicates that it may be possible to use this method for making reliable predictions about the relative thermal stability of other amorphous materials.

- The significantly higher thermal stability of the high-Si/C material is further shown by the fact that the bond lifetimes in this material at 2400 K are not only higher then the bond lifetimes in the low-Si/C material at 2400 K, but also higher than the bond lifetimes in the low-Si/C material at 1000 K.

- On the average, lifetimes are slightly higher for C-N, C-C and B-N bonds than for Si-N, Si-C and B-C bonds. This is probably due to the fact the atom pairs from the latter group form mainly single bonds, while atom pairs from the first group often form also double or even triple bonds which are generally stronger than the equivalent single bonds.

- The fact that lifetimes of the Si-containing bonds are not longer (even slightly shorter) than lifetimes of the C-containing bonds in the same material indicates that the higher thermal stability of high-Si/C materials is based on deeper structural phenomena than simply a difference in types of atoms bonded. In particular, it shows that the bond lifetime is not constant for a particular atom pair but depends also on the local environment of the atoms bonded.

### 8.3.2 Rates of \(N_2\) formation

It is known\(^1\) that a main mass-loss process which limits temperature stability of Si-(B)-C-N materials is the outflow of nitrogen due to the decomposition reactions \(\text{Si}_3\text{N}_4 + 3\text{C} \rightarrow 3\text{SiC} + 2\text{N}_2\) and \(\text{Si}_3\text{N}_4 \rightarrow 3\text{Si} + 2\text{N}_2\). Figure 8.8 shows rates of \(N_2\) formation in the low-Si/C samples \(\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{44}\) and \(\text{Si}_{11}\text{C}_{53}\text{N}_{44}\) and in the high-Si/C samples \(\text{Si}_{39}\text{B}_{14}\text{C}_{11}\text{N}_{44}\) and \(\text{Si}_{53}\text{C}_{11}\text{N}_{44}\). MD runs were performed after initial mixing of the low-Si/C pair of samples, while input structures of the latter pair of samples were obtained by replacing of all Si atoms by C atoms and vice versa (followed by optimising of a new wavefunction). Using the same N contents and atomic densities for all these samples ensure that the rate of \(N_2\) formation depends only on the Si/C/B compositions. Note than although the atomic densities used for the fictitious high-Si/C compositions are therefore probably slightly overestimated and it was shown in chapter 5 that rate of \(N_2\) formation can decrease as a result of higher coordination number at higher material density, the high-Si/C compositions simulated at experimental atomic densities (see e.g. section 8.1) have so high coordination numbers that they can hardly increase more as a result of higher atomic density.

As for the calculations described in chapter 5, a number of the N atoms start out statistically in close proximity and are therefore prone to form \(N_2\) molecules immediately. This leads to up to 4 \(N_2\) molecules at 1000 K where diffusion does not play a significant role in the \(N_2\) formation - see Fig. 8.8(a). These \(N_2\) molecules are not of relevance to the rate of \(N_2\) formation due to diffusion and bond-breaking processes. Figure 8.8(b) therefore shows only the numbers of \(N_2\) molecules formed by atoms which start far from each other in the initial (input) structure.
It can be seen from Fig. 8.8 that the numbers of N\textsubscript{2} molecules formed are significantly higher in the low-Si/C Si-(B)-C-N materials than in the equivalent (that is, with the same B and N contents and atomic densities) high-Si/C materials at all temperatures. This effect is stronger for Si-C-N than for Si-B-C-N materials, probably due to the difference in Si contents in the high-Si/C compositions Si\textsubscript{39}B\textsubscript{14}C\textsubscript{11}N\textsubscript{44} and Si\textsubscript{53}C\textsubscript{11}N\textsubscript{44} (all B replaced by Si).

Figure 8.8(b) further shows that rate of N\textsubscript{2} formation due to the diffusion and bond-breaking processes is significantly lower for Si-B-C-N materials than for the equivalent Si-C-N materials. This correlates with the prediction\textsuperscript{10} that the addition of B protects Si-C-N ceramics from decomposition via the reactions described above.

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{fig88}
\caption{Number of N\textsubscript{2} molecules formed in Si(B)CN samples during 500fs MD runs at various temperatures in low-Si/C samples (Si\textsubscript{11}B\textsubscript{14}C\textsubscript{39}N\textsubscript{44} and Si\textsubscript{11}C\textsubscript{53}N\textsubscript{44} - full symbols) and in high-Si/C samples Si\textsubscript{39}B\textsubscript{14}C\textsubscript{11}N\textsubscript{44} and Si\textsubscript{53}C\textsubscript{11}N\textsubscript{44} (Si\textsubscript{39}B\textsubscript{14}C\textsubscript{11}N\textsubscript{44} and Si\textsubscript{53}C\textsubscript{11}N\textsubscript{44} - empty symbols). Panel (a) includes all N\textsubscript{2} molecules formed. Panel (b) includes only N\textsubscript{2} molecules which arise from N atoms that don't start out in close proximity to one another.}
\end{figure}
8.3.3 Role of boron in the networks

Table 8.8: The local environments of B and Si atoms in Si-B-C-N material of composition Si<sub>11</sub>B<sub>14</sub>C<sub>39</sub>N<sub>44</sub> at the end of MD runs at 1000, 2000 and 3000 K. C, N and CN denote numbers of B/Si atoms bonded to C only, to N only and to both C and N, respectively. Results are shown in numbers of atoms (C, N and CN - upper rows) and in percentages of the total ([CN]/[C+N+CN] - lower rows).

<table>
<thead>
<tr>
<th>Temperature</th>
<th>Surrounded by B</th>
<th>Surrounded by Si</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C, 3N, 9CN</td>
<td>1C, 5N, 8CN</td>
</tr>
<tr>
<td>1000 K</td>
<td>2C, 3N, 9CN</td>
<td>1C, 5N, 8CN</td>
</tr>
<tr>
<td>2000 K</td>
<td>3C, 4N, 7CN</td>
<td>3C, 4N, 7CN</td>
</tr>
<tr>
<td>3000 K</td>
<td>3C, 4N, 7CN</td>
<td>3C, 4N, 7CN</td>
</tr>
</tbody>
</table>

Table 8.8 shows the role of B in stabilizing the Si-B-C-N sample of composition Si<sub>11</sub>B<sub>14</sub>C<sub>39</sub>N<sub>44</sub>. The sample consists mainly of C and N, and at high temperatures it would therefore tend to form graphitic zones while simultaneously releasing N<sub>2</sub> molecules. Table 8.8 compares the behaviour of B during these processes with Si (the other minor element in this composition) by observing the local environment of each of these atoms. When there are no Si-Si, B-B and Si-B bonds in this composition, each Si and B atom can be bonded to N only, C only or to both C and N. It can be seen that most of the Si atoms are bonded to both C and N, which suggests that they typically form bridges between segregated zones of C (stable graphite) and N (unstable source of N<sub>2</sub> molecules). On the contrary, boron atoms are several times more often bonded only to N or also only to C - in other words, they inhibit formation of pure C and especially pure N zones. This can inhibit formation of N<sub>2</sub> molecules and therefore increasing the thermal stability of the material as shown in figure 8.8(b).

Table 8.9: Selected structural data for Si-C-N and Si-B-C-N samples of composition Si<sub>11</sub>C<sub>53</sub>N<sub>36</sub> and Si<sub>11</sub>B<sub>14</sub>C<sub>39</sub>N<sub>44</sub> (denoted as low Si/C) and Si<sub>32</sub>C<sub>14</sub>N<sub>54</sub> and Si<sub>32</sub>B<sub>8</sub>C<sub>6</sub>N<sub>54</sub> (high Si/C). The columns show (1) number of Si-N bonds (all bond orders), (2) how many Si atoms are bonded only to N, and how many of them are bonded only to C and N atoms, (3) averaged nitrogen coordination number, (4) averaged total coordination number, (5) the percentage of N atoms with which a lonepair is associated, and (6) percentage of like bonds in a network.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Si-N bonds</th>
<th>surroundings of Si</th>
<th>coord. (N)</th>
<th>coord. (total)</th>
<th>lonepairs/ N at. (%)</th>
<th>like bonds (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si-C-N - low Si/C</td>
<td>26</td>
<td>1N, 9CN</td>
<td>2.42</td>
<td>2.88</td>
<td>81</td>
<td>34</td>
</tr>
<tr>
<td>Si-B-C-N - low Si/C</td>
<td>31</td>
<td>3N, 6CN</td>
<td>2.69</td>
<td>3.04</td>
<td>60</td>
<td>19</td>
</tr>
<tr>
<td>Si-C-N - high Si/C</td>
<td>109</td>
<td>17N, 9CN</td>
<td>2.70</td>
<td>3.11</td>
<td>78</td>
<td>7</td>
</tr>
<tr>
<td>Si-B-C-N - high Si/C</td>
<td>118</td>
<td>25N, 3CN</td>
<td>2.89</td>
<td>3.22</td>
<td>65</td>
<td>3</td>
</tr>
</tbody>
</table>

Table 8.9 shows structural differences resulting from replacing a proportion of the C atoms by B in Si-C-N samples whilst keeping constant the atomic density, cooling rate and using the same set of bonding distance cutoffs to identify bonds. As has been shown previously (in chapters 3 and 4 experimentally, in table 8.2 by simulations), the (newly added) boron forms a high number of bonds with nitrogen. However, the occupation of a fraction of the nitrogen bonding states by boron does not generally lead to a decrease of the
numbers of other N-containing bonds. Si-N, the most populated bond, is increased (see column 1 of table 8.9) due to a decrease in the number of Si-C bonds, resulting from the fact that a proportion of C was replaced by B which has very low affinity to Si. The result is a higher number of Si atoms bonded only to N (at practically constant Si coordination) - see column 2. The most important result in table 8.9 is an increase in average N coordination number due to the new B-N bonds (see column 3) and the consequent increase in total coordination number (at approximately constant coordinations of Si and C) - see column 4. This is possible because a proportion of the lonepairs associated with N atoms (see the networks in Fig. 8.1) are converted to bonding electrons (column 5) when B is added. Column 6 shows a decrease in the percentage of like (mainly C-C) bonds in the networks when some of the C atoms are replaced by B.

The demonstrated ability of boron to convert nitrogen lonepairs present in Si-C-N networks to bonding electrons has two important consequences:

1. a higher coordination number for the B-containing networks, leading to a higher bulk modulus and hardness (this prediction agrees well with experiment in that the Si-B-C-N materials\textsuperscript{5,11} have significantly higher hardness than do the Si-C-N materials prepared under equivalent conditions\textsuperscript{12,13}).

2. the higher coordination number is also likely to improve the thermal stability of the Si-B-C-N materials in comparison with Si-C-N materials because more bonds need to be broken before an atom can diffuse from one site to another.

8.3.4 Conclusions

Temperature stability was examined for Si-(B)-C-N materials of various Si/C ratios. It was shown that lifetimes of all major bonds are significantly longer in Si-B-C-N materials with higher Si/C ratios, despite the fact that at a given composition lifetimes of C-containing bonds are similar or even longer than lifetimes of Si-containing bonds. Calculations capturing the formation of N\textsubscript{2} molecules in materials show that both the addition of 14% of B into a Si-C-N material and increasing of the Si/C ratio in Si-(B)-C-N materials leads to inhibiting of N\textsubscript{2} formation. All of these results correlate with experimental observations showing exceptional thermal stability of high-Si/C Si-B-C-N materials. Higher network coordination number at higher B content (as well as at higher Si/C ratio) appears to be a reason for the impressive thermal stability. The differences in calculated results are significant, suggesting that ab-initio liquid quench simulations are suitable for reliable predictions of relative thermal stabilities of amorphous materials.
8.4 Optical properties and band gap

In this section, calculations of optical conductivities and band gaps are shown for samples of compositions:

- Si\textsubscript{14}B\textsubscript{23}C\textsubscript{6}N\textsubscript{55} (effect of number of unoccupied states considered).
- Si\textsubscript{11}B\textsubscript{14}C\textsubscript{39}N\textsubscript{36} and Si\textsubscript{32}B\textsubscript{8}C\textsubscript{6}N\textsubscript{54} (optical properties).
- Si\textsubscript{10}B\textsubscript{12}C\textsubscript{40}N\textsubscript{38}, Si\textsubscript{10}B\textsubscript{12}C\textsubscript{40}N\textsubscript{38}H\textsubscript{6} and Si\textsubscript{32}B\textsubscript{8}C\textsubscript{6}N\textsubscript{54} (band gaps). Here, the high-Si composition is the same as used for calculations of optical properties; the low-Si composition is slightly different because it resulted from averaging over samples deposited with various values of substrate bias.

The composition with non-negligible H content refers to a sample deposited with \( U_b = -100 \) V, the other compositions refer to samples prepared with \( U_b = -500 \) V where the experimental H content was significantly reduced.

8.4.1 Related experimental results

Ref. 14 shows measured values of the extinction coefficient and the refractive index for various Si-C-B-N compositions in the range \( \lambda = 300 - 1700 \) nm. Films with high Si content exhibited low values of the extinction coefficient (significantly decreasing with \( \lambda \)) and refractive index 1.8 - 2.1 (decreasing with \( \lambda \)). Films with high C content exhibited high values of the extinction coefficient (slowly decreasing with \( \lambda \)) and refractive index 1.9 - 2.2 (increasing with \( \lambda \)). The observed dependence of the extinction coefficient (and thus the photoconductivity) on the Si/C ratio in the films indicates that the band gap in the Si-B-C-N materials studied increases significantly with increasing Si/C ratio. This is also indicated by the measurements of electrical conductivity of Si-B-C-N materials (see the discussion in chapter 4). In summary experimental work has shown that:

- Si-C-B-N materials are insulators at high Si/C ratio while they have conductivity of the same order as semiconductors at low Si/C ratio.
- For samples with low content of implanted Ar, the electrical conductivity increases with increasing value of the negative substrate bias \( |U_b| \), which is probably related to decreasing hydrogen content with increasing \( |U_b| \).

These results are consistent with an increase of the band gap with increasing Si/C ratio and with increasing H content in materials.

8.4.2 Related theory - the Kubo-Greenwood formula

The relations between (real part of) the photoconductivity \( \sigma \), the absorption coefficient \( \alpha \), the extinction coefficient \( k \), the refractive index \( n \), the wavelength \( \lambda \), the angular frequency \( \omega \), the speed of light \( c \) and the permittivity \( \varepsilon_0 \) are:

- \( \alpha = \sigma/\varepsilon_0 n c \) (often used is for some reason also \( \alpha = 4\pi\sigma/nc \) which is in Gaussian - not SI - system of units)
- \( k = \alpha \lambda/4\pi = \sigma \lambda/4\varepsilon_0 n c = \sigma/2\varepsilon_0 n \omega \)

Once we know the electronic structure of a material, the real part of the conductivity can be calculated for given \( \omega \) using the Kubo-Greenwood formula\textsuperscript{15,16}:

\[
\sigma(\omega) = \frac{2n^2}{3m^2} \sum_{n,m} \sum_{\alpha=x,y,z} (f_m - f_n) \left| \psi_n \right| p_{\alpha} \left| \psi_n \right|^2 \delta(E_n - E_m - \hbar\omega) \quad (Eq. 8.3)
\]
where $\psi$, $E$ and $f$ are eigenfunctions, their eigenvalues and the occupation numbers, respectively, and $\Omega$ is the volume of the supercell. It is well known in density-functional theory that the calculated Kohn-Sham eigenvalues and related transition energies do not represent the true electronic transitions. In particular, the Kohn-Sham gaps tend to be too small. Despite this limitation, this formalism has been reported to give correct trends or even a semiquantitative agreement with an experiment.

The electronic structure of an amorphous semiconductor also allows us to calculate the optical gap ("Tauc gap") $E_{\text{opt}}$ of such material from the formula

$$h\omega \sqrt{\varepsilon} = B(h\omega - E_{\text{opt}})$$

(Eq. 8.4)

where $B$ is a constant. The dielectric permittivity $\varepsilon$ can be calculated from the convolution integral

$$\varepsilon = \frac{1}{\omega^2} \int g_0(E)g_u(E + \hbar\omega)dE$$

(Eq. 8.5)

where $g_0$ and $g_u$ are densities of occupied and unoccupied states below and above the Fermi energy, respectively.

8.4.3 Interpretation of calculated photoconductivity

Figure 8.9 shows the effect of the number of unoccupied states included in the calculation on the calculated photoconductivity of the simulated sample $\text{Si}_{14}\text{B}_{23}\text{C}_{6}\text{N}_{55}$. In addition to 212 occupied two-electron Kohn-Sham states, which resulted from the paired-spin approach used in the simulation, another 10-100 unoccupied states were used for the calculation. It can be seen that to obtain a value of the calculated photoconductivity which is independent of the number of unoccupied states considered, the number of unoccupied states needed increases with increasing photon energy. Although the exact (unoccupied states needed)/(occupied states) ratio may differ for various compositions, results shown Figs. 8.10-8.12 were obtained with 100 unoccupied states in addition to 211 - 223 occupied states, which is more than enough for completely reliable results in the range where the optical properties were investigated experimentally ($\lambda \geq 300$ nm - that is, energy $\leq 4$ eV).

![Figure 8.9: Calculated photoconductivity of the material of composition $\text{Si}_{14}\text{B}_{23}\text{C}_{6}\text{N}_{55}$. Numbers 10 - 100 indicate numbers of empty Kohn-Sham states included in the calculation performed using a 98-atom cell.](image-url)
Figure 8.10(a) shows a typical dependence of the photoconductivity $\sigma$ on $\lambda$. What can be seen is the characteristic decrease of $\sigma$ to zero (i.e. increasing material transparency) with $\lambda$ increasing up to $\sim 1000$ nm, due to decreasing photon energy to values lower that the band gap. The considerable noise below 1000 nm is caused by the limited number of atoms ($\sim 100$) in the simulation cell, while for example there are $\sim10^{17}$/mm$^2$ atoms in deposited samples used for experimental measurements of $\sigma$. For the same reason, there are calculated zero values of $\sigma$ interrupted by several non-zero responses (instead of a smooth close-to-zero dependence) at high values of $\lambda$ where the material is transparent.

![Graph](image)

**Fig. 8.10:** Calculated photoconductivity of material of composition Si$_{11}$B$_{14}$C$_{39}$N$_{36}$. Panel (a) shows results calculated with energy (i.e. frequency) steps of 0.1 eV. Panel (b) shows results calculated with energy steps of 0.01 eV.

Figure 8.10(b) shows the effect of the steps used for sampling the energy (i.e. frequency) on the results. Below the limit where $\sigma$ has non-zero values only, the 10 times more frequent sampling caused much higher deviation of calculated $\sigma$ values but did not affect averaged values or trendlines. Averaged calculated value of $\sigma$ between 2 - 4 eV (300 - 600 nm) is in this case 173.7 $\Omega^{-1}$mm$^{-1}$ for energy steps of 0.1 eV and 174.9 $\Omega^{-1}$mm$^{-1}$ for energy steps of 0.01 eV which constitutes a difference of less than 1 %. However, in the range where $\sigma$ has mostly zero values, the intensity of the few responses observed is proportional to $1/(energy$ $step)$. It can be concluded that while numbers and amplitudes of these freestanding responses can be probably used for qualitative comparing of various samples and their levels of transparency, their amplitudes cannot be compared with those in the range where $\sigma$ has non-zero values only.
8.4.4 Calculated photoconductivity

Figures 8.11 and 8.12 compare calculated and experimental (measured between $\lambda = 300$ and 1700 nm) photoconductivity of two Si-B-C-N samples of composition $\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}$ (semiconductor, opaque in visible spectra) and $\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}$ (insulator, transparent - slightly yellow - in visible spectra). Because of the noise, exponential-decay trendlines are provided together with the calculated values.

Due to the smaller Kohn-Sham gaps, underestimated for fundamental reasons by the DFT, photons are more likely to be absorbed in the electronic transitions, which increases the calculated photoconductivity. This phenomenon is more significant for materials with large band gaps, while it is less important for materials with small or even zero band gaps. In accordance with this expectation, the calculated $\sigma$ values for the semiconductive material $\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}$ were in the same order as the experimental ones (on the average 2.75 times higher in the range shown), while the calculated $\sigma$ values for the insulating material $\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}$ were almost two orders of magnitude higher than the experimental ones (on the average 80 times higher in the range shown). Presented calculated data are divided by these factors in order to allow comparing of shapes of the dependencies.

![Photoconductivity graph](image)

**Fig. 8.11:** Photoconductivity of material of composition $\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}$. Panel (a) shows calculated values divided by a factor of 2.75 and a exponential-decay trendline. Panel (b) shows experimental values measured between $\lambda = 300$ and 1700 nm.
A phenomenon complementary to the previous one can be seen from comparison of shapes of the dependencies $\sigma(\lambda)$. For the material $\text{Si}_{11}\text{B}_{14}\text{C}_{39}\text{N}_{36}$ where both the experimental and DFT band gaps are narrow and thus close to each other (Fig. 8.11), the shapes of the experimental and calculated dependencies of $\sigma(\lambda)$ are very similar. In particular, both of them indicate that $\sigma(\lambda)$ starts to increase significantly with decreasing $\lambda$ for $\lambda < \sim1100$ nm. This is in accordance with opacity of this material in visible spectra ($\lambda < 800$ nm).

On the other hand, the calculated and experimental dependencies differ for the material $\text{Si}_{32}\text{B}_{8}\text{C}_{6}\text{N}_{54}$ where the experimental band gap is much larger than the DFT band gap. In particular, the calculated dependence $\sigma(\lambda)$ starts to increase with decreasing $\lambda$ sooner (at $\lambda < 700 - 800$ nm: Fig. 8.12(a)) than the experimental dependence ($\lambda < 500$ nm: Fig. 8.12(b)). This is again due to the easier electronic transitions activated by phonons with $\lambda = 500 - 800$ nm over the narrow DFT band gap, while in the experiment such transitions are possible below 500 nm only. Absorption of blue light ($\lambda < 500$ nm) in the material and its transparency in the other parts of the visible spectrum (i.e. green and red) result in the yellow (corresponding to green + red) colour observed.

![Fig. 8.12: Photoconductivity of material of composition Si$_{32}$B$_8$C$_6$N$_{54}$. Panel (a) shows calculated values divided by a factor of 80 and a exponential-decay trendline. Panel (b) shows experimental values measured between $\lambda = 300$ and 1700 nm.](image-url)
8.4.5 Calculated electronic density of states

Figure 8.13 shows calculated electronic density of states (EDOS) for Si-B-C-N materials with low Si/C ratio with \((\text{Si}_{10}\text{B}_{12}\text{C}_{40}\text{N}_{38}\text{H}_6)\) and without \((\text{Si}_{10}\text{B}_{12}\text{C}_{40}\text{N}_{38})\) hydrogen, and with high Si/C ratio \((\text{Si}_{32}\text{B}_{8}\text{C}_6\text{N}_{54})\). Figure 8.13(a) shows complete band structures of the materials, while Fig. 8.13(b) shows only EDOS around averaged the Fermi energies calculated. Around the Fermi energy it can be seen that the EDOS is slightly lower for the hydrogenated low-Si sample than for the non-hydrogenated one, and especially that the EDOS is much lower for the high-Si sample than for the low-Si ones. We quantify the results by calculating of two quantities, which can be used as a measure of the band gap:

- the Tauc gap introduced above.
- the "10-states interval": averaged width of the energy interval, which includes 5 highest occupied and 5 lowest unoccupied states. These intervals are comparable due to the similar numbers of occupied states in the simulation cells for all samples shown.

![Graph showing EDOS for different Si/C ratios](image)

**Fig. 8.13**: The electronic density of states (EDOS) for Si-B-C-N materials with low Si/C ratio with \((\text{Si}_{10}\text{B}_{12}\text{C}_{40}\text{N}_{38}\text{H}_6)\) and without \((\text{Si}_{10}\text{B}_{12}\text{C}_{40}\text{N}_{38})\) hydrogen, and with high Si/C ratio \((\text{Si}_{32}\text{B}_{8}\text{C}_6\text{N}_{54})\). Results are averaged over 13 snapshots obtained during the 500 fs production run. Panel (a) includes all occupied and part of the unoccupied states. Panel (b) shows EDOS around averaged Fermi energy only.
Table 8.9: Tauc gap and averaged width of the energy interval, which includes 5 highest occupied and 5 lowest unoccupied states (the 10-states interval) for low Si/C ratio Si-B-C-N materials with (Si$_{10}$B$_{12}$C$_{40}$N$_{38}$H$_{6}$) and without (Si$_{10}$B$_{12}$C$_{40}$N$_{38}$) hydrogen, and with high Si/C ratio (Si$_{32}$B$_{8}$C$_{6}$N$_{34}$).

The main reason for introducing the second quantity is the relatively large error associated with calculated Tauc gaps. These errors can be up to 100% in cases when the line fitted to the linear part of the Equation 8.4 plot crosses the vertical axis very close to zero.

The results are summarized in table 8.9. It can be seen that:

• as expected for the reasons discussed above, the Tauc gaps are underestimated by the DFT simulations, having small or even negative values. They can therefore only be used for comparative purposes.
• despite the relatively large error bars of the Tauc gaps, both quantities calculated give the same trends.
• the trends given are in agreement with the expectations (increase of the band gap with increasing Si/C ratio, and also slight increase of the band gap after addition of H into the material). These results can be therefore regarded as complementary to the calculations of photoconductivity.

8.4.6 Conclusions

It has been confirmed that the calculations of EDOS and related quantities give the correct trends when comparing materials of different compositions and thus are able to give reliable predictions concerning the influence of individual elements on optical and electrical characteristics of amorphous materials. The predictions are semiquantitatively correct (including correct determination of the $\lambda$ limit between absorbed and transmitted wavelengths) for narrow band gap materials only. Underestimation of the band gap can affect the quantitative results significantly for large band gap materials.
8.5 References

2. www.webelements.com
Chapter 9 - Conclusions

9 Conclusions

The thesis reports on results obtained in years 2002-2006 in the laboratories of the Department of Physics at the University of West Bohemia (Czech Republic) and of the Department of Applied and Plasma Physics at the School of Physics, University of Sydney (Australia). The results presented in chapters 3-8 fulfil the thesis aims as documented in chapter 1.

New hard and highly thermally stable amorphous Si-B-C-N materials have been synthesized and computer simulations of their structures performed. The materials have been shown to have a unique combination of properties making them ideal candidates for applications in areas such as protective coating technologies, microelectronics or the production of thermally stable fibers for composites. The effects of plasma parameters during the film formation process have been investigated and optimized with respect to film properties such as hardness and thermal stability. Atomistic simulations have been used to explain the dependencies observed.

9.1 Main experimental conclusions

The first part of the thesis deals with the experimental preparation and characterization of the new quaternary Si-B-C-N materials, deposited in the form of thin films by reactive magnetron sputtering. The main conclusions of this part of the research can be summarized as follows.

(1) A series of novel quaternary Si-B-C-N materials in the form of thin films were prepared by reactive magnetron sputtering of composite C-Si-B or B₄C-Si targets in N₂–Ar gas mixtures. The technique used proved to be suitable for reproducible synthesis of these materials. A number of B-C-N and Si-B-C films were also prepared for comparison. The Si-B-C-N films were generally found to be amorphous with low compressive stress and good adhesion to silicon or glass substrates. The process and film characteristics were controlled by varying the sputter target composition (0-75 % Si in a target erosion area at a fixed 20 % B fraction in the C-Si-B target erosion area). The Ar fraction of the N₂–Ar gas mixture was varied between 0 and 100 %. The effect of negative rf-induced substrate bias, Uᵦ, was investigated in the range between floating potential and -700 V, and the effects of substrate temperatures up to 350 °C (occasionally up to 700 °C) were studied.

(2) Deposition carried out using a target with a high Si fraction (60-75 %) in the sputtered target erosion area, leading to high Si/C ratios in the films, were found to be optimum for producing dense covalently bonded insulating materials with high hardness (up to 47 GPa), high elastic recovery (up to 88 %) and low compressive stress. It was shown that silicon relieves compressive stress generated by implanted Ar atoms in these materials. On the other hand, films created with a high C fraction (75 %) in the sputtered target erosion area, which have low Si/C ratios, were found to be semiconductive materials with conductivity controllable over a wide range.

(3) The discharge gas mixture composition was found to be an important process parameter for the deposition of Si-B-C-N materials due to the (a) different sputtering yields of target materials by argon and nitrogen, which affect the elemental composition and deposition rate, (b) stronger bombardment of growing films at higher Ar content in N₂–Ar gas mixture as shown by measurements of powers absorbed in the
discharge, affects the hardness and deposition rate of the materials, and (c) processes implicated by implanted argon atoms. In particular, high Ar content in N$_2$-Ar gas mixture was found to increase the hardness of the high-Si/C materials, and to increase compressive stress and decrease electrical conductivity (especially at high |$U_b$|) of the low-Si/C materials.

(4) Negative substrate bias voltage, $U_b$, has been shown to be useful in controlling the characteristics of films of very similar Si-B-C-N compositions. In particular, the low |$U_b$| value, $U_b = -100$ V, with the corresponding low values of the ion-to-film-forming particles flux ratio $\Gamma_i/\Gamma_p \leq 0.2$ and low ion energy per deposited atom $E_{in} \leq 20$ eV are optimum for the formation of high-Si/C films with maximum hardness and elastic recovery when a gas mixture with high Ar content is used. On the contrary, increasing |$U_b$| values were observed to improve the electrical conductivity of the low-Si/C films with low content of implanted Ar.

(5) Furthermore it was shown that increasing substrate temperature improves the mechanical properties of the high-Si/C materials, while at decreasing Si/C ratio this effect becomes weaker or even inverse.

9.2 Main simulation conclusions

The second part of the thesis presents the results of ab-initio computer simulations of structures approximating the experimentally prepared (Si)-(B)-C-N materials. The simulations were performed using a liquid quench algorithm implemented in Car-Parrinello molecular dynamics. The main conclusions of this research can be summarized as follows.

(1) The formation of free N$_2$ molecules was observed in the liquid quench simulations of (Si)-(B)-C-N amorphous materials and a temperature window (with a peak at 5000 K) in which stable N$_2$ molecules are formed was identified. The results predict that the final content of nitrogen incorporated in networks of given Si/B/C ratios increases with the cooling rate (due to the shorter time spent in the active temperature window for N$_2$ formation) and increases with the density of the material (due to higher coordination numbers inhibiting N diffusion and subsequent formation of N$_2$). The results further suggest that at constant temperature and atomic density the rate of N$_2$-formation in Si/B/C-containing materials decreases with increasing Si-content. This explains the ability of Si to enhance the final N-content in experimentally prepared materials. A modified liquid-quench algorithm, which begins with a sufficient N-excess and progressively removes N$_2$ molecules as they form in the simulation cell, has been developed to simulate the diffusion of N$_2$ from the structure during film synthesis.

(2) When implanted Ar atoms were included in the simulations of Si-B-C-N materials, we observed a segregation of a Si-rich phase around them. The energy advantage gained by surrounding Ar atoms with longer and more flexible Si-containing bonds was proposed to be a driving force for this segregation. The process was shown to be temperature-dependent with a maximal effectiveness at 1000-1500 K. Although it was found that the samples with higher Ar content (corresponding to films deposited with high |$U_b$|) are not far from homogenous (most of the network atoms were close to at least one Ar atom), the samples with low Ar levels (corresponding to films deposited with low |$U_b$|) were predicted to be heterogeneous. The heterogeneous low Ar materials had Si-rich regions close to the Ar atoms and Si-poor regions elsewhere.
This predicted segregation correlates with and can be used to explain several experimentally observed phenomena, including (a) hardening of annealed materials due to the identical temperature dependence of both the hardening and the segregation processes, (b) increased material hardness at $U_b = -100$ V compared with $U_b = -500$ V for films prepared with high (75%) Ar fraction in N$_2$-Ar gas mixture, (c) an increasingly positive effect of substrate temperature on hardness with increasing content of (segregating) Si in the films, and (d) the ability of Si to relieve stress generated by the implanted Ar atoms.

(3) In accordance with experimental (XPS and IR) results, the most highly populated bonds in the simulated Si-B-C-N materials with high-Si/C ratio were found to be Si-N (mostly single), B-N (single and double) and C-N (all bond orders). In the compositions with low-Si/C, the following bond types were also significant: C-Si (single), C-B (single) and C-C (single and double). A method to calculate bond ionicities, $\lambda$, using Wannier function centres (WFCs) was developed. Typical values calculated are 0.1-0.3 for homonuclear bonds, 0.4-1.0 for heteronuclear single bonds and 1.0-2.0 for heteronuclear double bonds. Calculated bond ionicities and atomic charges were shown to be in accordance with known electronegativities of atoms.

(4) An investigation of the effects of B and the Si/C ratio on the characteristics of Si-(B)-C-N materials was carried out. The inclusion of B, which bonds preferentially to N, results in the conversion of lonepairs of valence electrons associated with N atoms to bonding electrons, significantly increasing the averaged nitrogen coordination number. Carbon was found to form a significant number of multiple bonds whereas silicon tended to form single bonds. This resulted in higher network coordination numbers in networks with high Si/C ratio (despite same number of valence electrons of Si and C). Thus high Si/C ratio and non-zero B content (even when B replaces C which has more valence electrons) both lead to improved mechanical properties as well as thermal stability of the coatings, in agreement with experimental results.

(5) High-temperature stability of simulated materials was examined also by two direct methods. It was shown that lifetimes of all major bonds are significantly longer in higher-Si/C Si-B-C-N composition, despite the fact that at a given composition lifetimes of C-containing bonds are similar or even longer than lifetimes of Si-containing bonds. Calculations capturing formation of N$_2$ molecules in a material (indicating its decomposition) have shown that both the addition of B into a Si-C-N material and increasing of the Si/C ratio in Si-(B)-C-N materials lead to inhibiting of N$_2$ formation.

9.3 Applicability of the simulation method used

Experience obtained during liquid-quench MD simulations of amorphous materials and comparison of the results with experiment is summarised below for individual material characteristics. Both the successes and failures of the method used are included.

Material structure and roles of atoms
- The method used has been shown to be very successful in describing structures of materials and the processes taking place there, providing information not accessible experimentally. The phenomena examined include segregation into zones of different compositions, the formation of free molecules, bonding preferences of individual atom
types or preferences of valence electrons to form bonds or lonepairs. It has been shown that for obtaining exact results in this field, all the atoms present (including e.g. apparently negligible few percent of implanted inert argon) usually have to be included in the simulation.

- In contrast to monoatomic materials, such as a-C with structures, previously characterized by a few quantities (coordination numbers, numbers of network rings), the statistical information available here can provide a variety of interesting but complex results including bonding statistics, distributions of distances between atoms of various types, numbers of lonepairs associated with individual atom types or surroundings of (sets of atoms bonded to) individual atom types. Further information can be provided by visual inspection of the structures.

- On the other hand, the simulation algorithm used cannot capture processes that take place at long ($\geq 10$ps) time scales (such as crystallization or diffusion of free gas molecules formed to the surface).

### Bonding statistics and bond characteristics

- The calculated bonding statistics correlate very well with the experimental results, including in cases when they are very far from a "random network" (see for example the very low or zero number of Si-Si bonds even at a high Si content).

- Bond length and bond ionicities as indicated by Wannier function centers (WFCs) correlate with predictions given by reported covalent radii and electronegativities of individual atom types for the pseudopotentials and energy cutoff used. The method presented for the calculation of a covalent bond ionicity however needs to be tested also for some more ionic amorphous materials.

- Occasional problems in the quantification of the bonding were encountered due to the difficulty associated with selecting bond distance cutoffs when the first and second peak of an atom-WFC partial distribution function are not well distinguished (most likely for Si). Moreover, finding of a bond order may be difficult when all WFCs are close to a particular atom and some of them could therefore be a lonepair (most likely for the short and relatively ionic $\text{C}≡\text{N}$ bond).

### Stress and mechanical properties

- It has been already shown previously that correct values of stress can be calculated by the simulation method used. However, our results suggest that a very exact knowledge not only of elemental composition, but also of materials density is necessary for this to be achieved. Sufficiently accurate material densities are often not available for disordered amorphous materials, which makes the direct stress calculations probably more useful for crystalline materials. A similar statement can be made for bulk modulus (for which roughly correct data were nevertheless successfully obtained, but without any additional information not accessible experimentally).

- The high credibility of calculated structural and bonding data makes them very useful for many qualitative predictions based on characteristics which are known to affect mechanical properties (coordination numbers, bond lengths or bond ionicities).

### Electronic structure and photoconductivity

- It is well known that due to the smaller Kohn-Sham gaps, underestimated for fundamental reasons by DFT, photons are more likely to be absorbed in the electronic transitions, which increases the calculated photoconductivity. Typically the calculated characteristics related to the material electronic structure (photoconductivity, Tauc gap
Chapter 9 - Conclusions

or the interval containing 5 highest occupied and 5 lowest unoccupied states) are therefore in mutual agreement, but they do not agree with experimental values.

- The results suggest that this phenomenon is more significant for materials with a large band gap, while it is less important for materials with a small or even zero band gap. For the latter narrow band gap materials, the predictions can be semiquantitatively correct (including, for example, the correct determination of the \( \lambda \) limit between absorbed and transmitted wavelengths when calculating the photoconductivity).

- Nevertheless, the method has been shown to give the correct trends, which allows reliable predictions to be made on the qualitative behaviour of the band gap and related characteristics.

Temperature-dependent characteristics

- The method used has been shown to be very successful for finding of temperature dependence of various phenomena. Characteristics successfully directly examined at various temperatures include segregation in the materials around implanted Ar atoms and the evolution of \( \text{N}_2 \) molecules.

- Observation of lifetimes of bonds (which, contrary to simulated crystalline materials, break and form again at sufficiently short time scales even at low temperatures) was shown to be suitable for examining the temperature stability of materials or of \( \text{N}_2 \) molecules formed in them. Due to the large differences in quantities of interest, the results obtained can be relatively easily and reliably interpreted.
Publications of the candidate

Refereed Journal Papers


Conference Papers and Proceedings (personal participation)


Conference Papers and Proceedings (work-fellow participation)


New quaternary amorphous materials Si-B-C-N: reactive magnetron sputtering and an ab-initio study

First part of the thesis is focused on experimental preparation of new hard quaternary amorphous materials Si-B-C-N with high thermal stability. Materials were prepared in the form of thin films using reactive magnetron sputtering. The technique used proved to be suitable for reproducible synthesis of these materials. The Si-B-C-N films were generally found to be amorphous with low compressive stress and good adhesion to silicon or glass substrates. The process and film characteristics were controlled by varying the sputter target composition, the Ar fraction in the N₂–Ar gas mixture, the negative rf-induced substrate bias, and the substrate temperature. Main conclusions describe the relationships between process parameters, discharge and deposition characteristics and film properties (elemental composition, chemical bonding structure, material hardness, compressive stress or electrical conductivity of materials prepared).

Second part of the thesis is focused on ab-initio simulations of structures of experimentally prepared Si-B-C-N materials. In the performed liquid-quench simulations, the Kohn-Sham equations for the valence electrons are expanded in a basis of plane wave functions, while core electrons were represented using Goedecker-type pseudopotentials. We simplified the ion bombardment process by assuming that the primary impact creates a localized molten region of high temperature and sufficiently short cooling time, commonly referred to as a thermal spike. Main conclusions deal with N₂ formation in studied materials, effect of implanted Ar on structure and properties of prepared materials, ability of Si to relieve that part of compressive stress which is caused by implanted Ar, and ability of B to improve thermal stability of Si-B-C-N materials. The calculated results are compared with experiment.

Nové kvaternární amorfní materiály Si-B-C-N: reaktivní magnetronové naprašování a ab-initio studie

První část disertace se zabývá experimentálním vytvářením nových tvrdých kvaternárních amorfních materiálů Si-B-C-N s vysokou teplotní stabilitou. Materiály byly připravovány ve formě tenkých vrstev pomocí reaktivního magnetronového naprašování. Použitá metoda se ukázala jako velmi vhodná pro reprodukovatelnou přípravu těchto materiálů. Vytvořené materiály Si-B-C-N byly obecně amorfní s nízkým kompresním pnutím a dobrou adhezí ke křemíkovým i skleněným substrátům. Depoziční proces a vlastnosti vytvořených materiálů byly řízeny složením rozprašovaného terče, složením výbojové směsi N₂–Ar, negativním rf předpětím na substrátech a teplotou substrátů. Hlavní závěry popisují vztahy mezi procesními parametry, charakteristikami depozičního procesu a vlastnostmi vytvořených materiálů (prvkové složení, vazebná struktura, kompresní pnutí a elektrická vodivost).

Druhá část disertace se zabývá ab-initio výpočty struktur experimentálně připravených materiálů Si-B-C-N, pomocí tzv. liquid-quench simulaci algoritmu. Kohn-Shamovy rovnice pro valenční elektrony byly řešeny s využitím rozložení vlnové funkce valenčních elektronů na rovinné vlny, zatímco jádra atomů a vnitřní elektronové orbitály byly popsány pomocí Goedeckerových pseudopotenciálů. Iontový bombard byl zjednodušen popsán na základě předpokladu, že dopad iontu vede k lokálnímu roztažení a následnému dostatečně rychlému zchladzení malého objemu materiálu – tzv. thermal spike. Hlavní závěry popisují vytváření molekul N₂ ve studovaných materiálech, vliv implantovaných atomů Ar na jejich strukturu a vlastnosti, schopnost Si snížit kompresní pnutí indukované atomy Ar, a schopnost B zvýšit teplotní stabilitu materiálů Si-B-C-N. Vypočítané výsledky jsou porovnávány s experimentálními.